

7th International and 22nd National Conference on Machines and Mechanisms

Convention Center, IIT Hyderabad, December 7–10, 2025



Compliant mechanism in front of my office by Cees van der Geer

Precision Compliant Mechanisms

Just Herder
Delft University of Technology

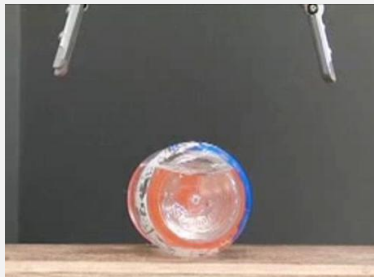
7th International and 22nd National Conference on Machines and Mechanisms

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Compliant mechanism in front of my office by Cees van der Geer

Remembrance of Prof. Ashok Midha
Characteristics of compliant mechanisms
Strategies to improve behavior
Trends and prospects



Underactuation

Mechanically adaptive grippers



Dynamic balancing

Fast and accurate manipulators



Delft

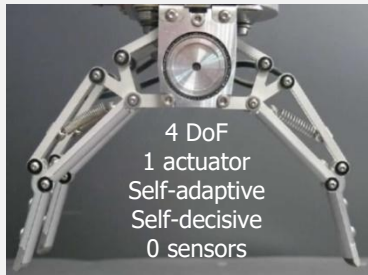
Parallel robotics

Light-weight and stiff



Static balancing

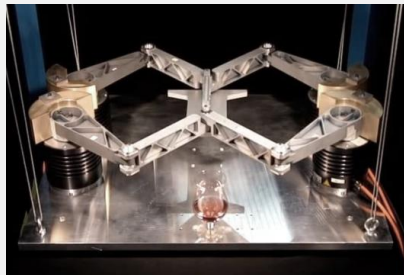
Adjustable spring mechanisms



4 DoF
1 actuator
Self-adaptive
Self-decisive
0 sensors

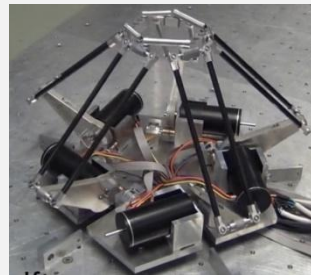
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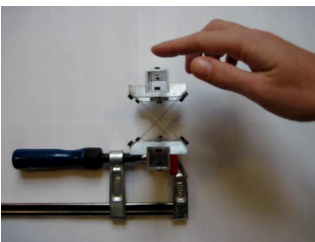
Parallel robotics

Light-weight and stiff



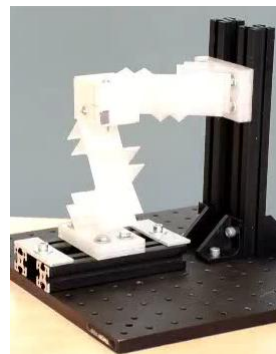
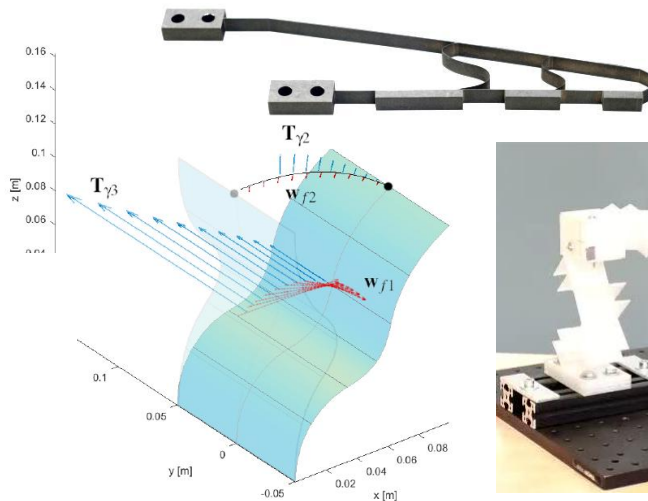
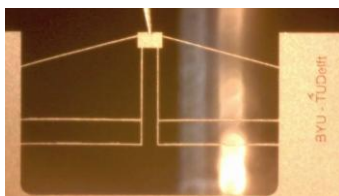
Static balancing

Adjustable spring mechanisms



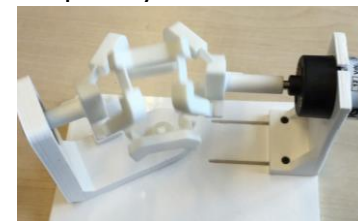
Compliant mechanisms

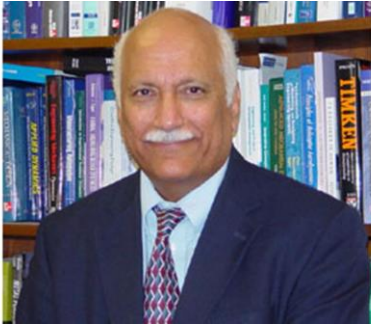
Precision motion and force transfer



Shell mechanisms

Spatially curved flexures

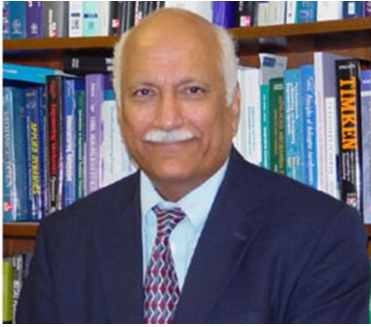




Prof. Ashok Midha

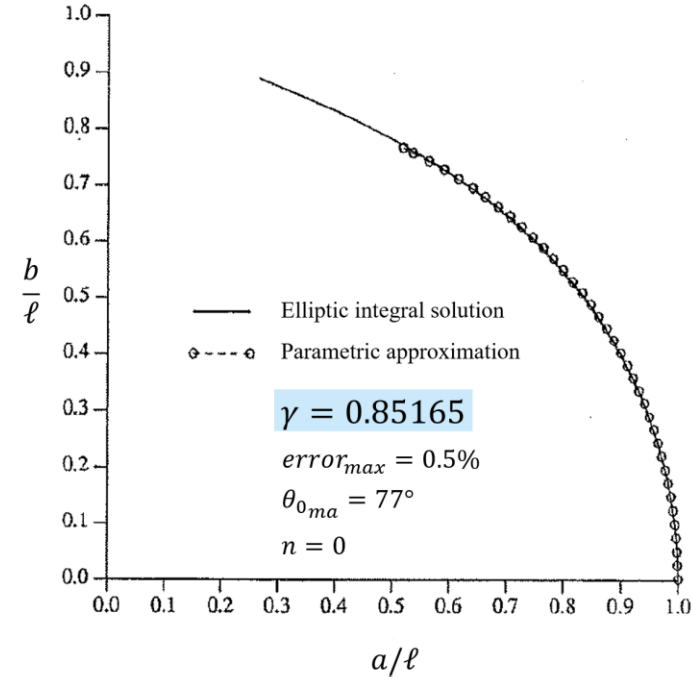
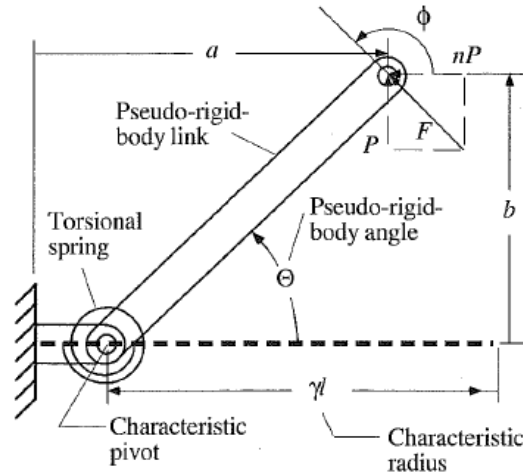
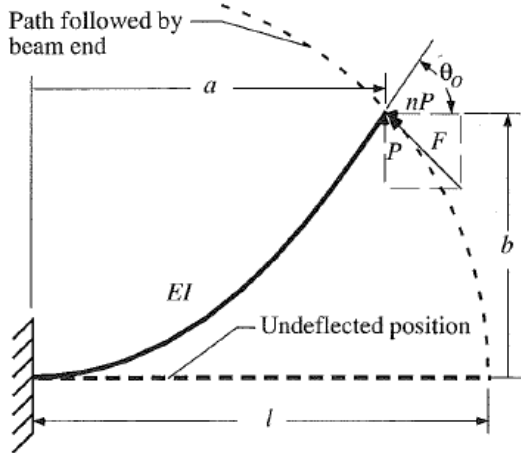
Prof. Ashok Midha
1946-2023

- B.Sc. National Institute of Technology in Jamshedpur in 1968
- M.Sc. 1970 and Ph.D. 1977 in Mechanical Engineering from the University of Minnesota
- Professor at Michigan Technological Institute, Pennsylvania State University, Purdue University, and The Missouri University of Science and Technology
- Head of Department at The Missouri University of Science and Technology for 10 years
- Over 140 papers in developing phase of the field of compliant mechanisms (“Father of Compliant Mechanisms”)
- Since 2012, ASME named a symposium within IDETC Mechanisms and Robotics after him
- Since 2024, ASME named the Compliant Mechanisms Award (that he installed and sponsored for years) after him
- ASME Fellow (since 2002) and received ASME Mechanisms and Robotics Award (1998)



Prof. Ashok Midha
1946-2023

Pseudo-Rigid Body Modeling (PRBM)





pecified Beam End Displacements

se 1: A three degree-of-freedom analysis
problem (specification of beam end horizontal
position a , vertical displacement b , and angle

se 2: A two degree-of-freedom analysis





N.N., Larry Howell, Charles Kim, Just Herder, Ashok Midha, Jonathan Hopkins, Guimin Chen, N.N., Dannis Brouwer, N.N.

Precision Compliant Mechanisms

Just Herder

Characteristics of compliant mechanisms

Well-behaved flexures

Strategies to improve behavior

Static balancing

Trends and prospects

Nature: compliant and strong



Compliant mechanisms

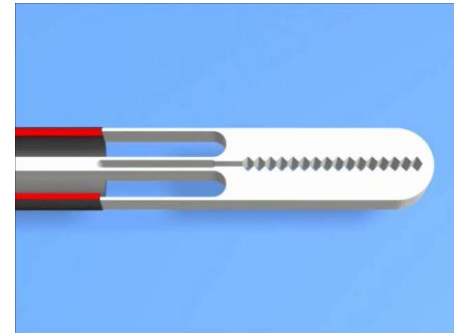
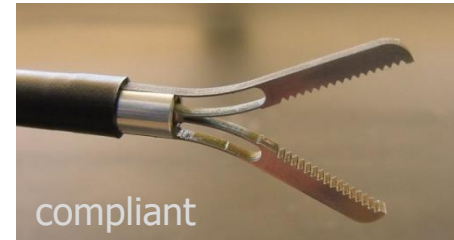
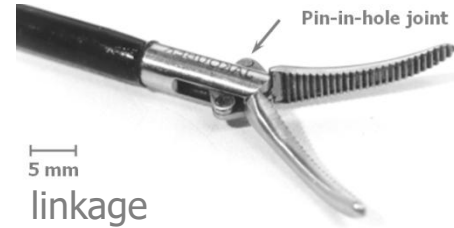
Motion due to deformation

- Flexible AND strong

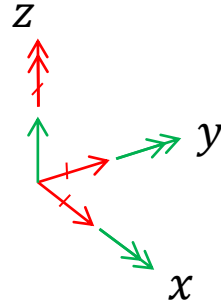
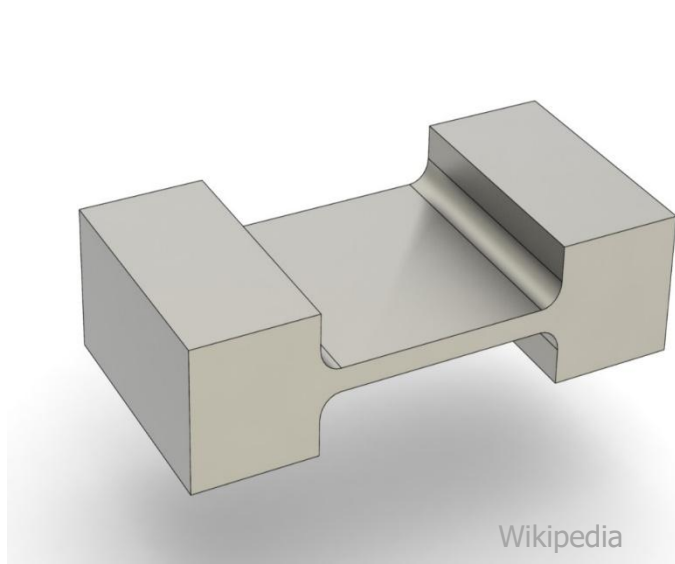
Essentially monolithic

- No friction or backlash
- No assembly or maintenance
- Simpler AND better

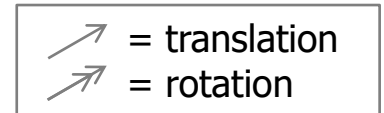
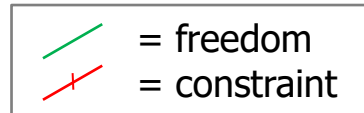
Kinematics and kinetics intertwined
Design more complicated and tailored
Finite support stiffness (ideally infinite)
Finite motion stiffness (ideally zero)



Flexure as a revolute joint



k_f = freedom stiffness, DoF
 k_c = constraint stiffness, DoC



Traditional analysis

Bernoulli-Euler
beam theory:

$$M = EI \frac{d\theta}{ds} \approx EI \frac{d^2y}{dx^2}$$

$$M = F(l-x) \quad \downarrow \quad \theta = \frac{dy}{dx}$$

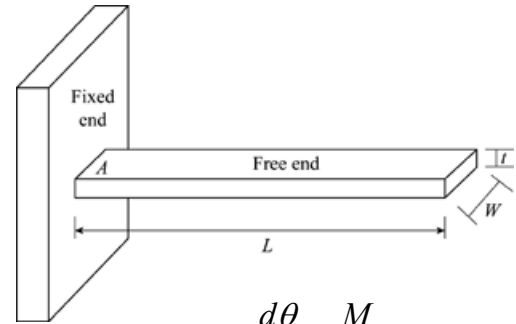
$$F(L-x) = EI \frac{d\theta}{dx}$$

Separating variables and integrating: $\theta = \frac{F}{EI} \left(Lx - \frac{x^2}{2} \right) + C$

Boundary conditions $\theta=0$ at $x=0$: $\theta = \frac{dy}{dx} = \frac{Fx}{2EI} (2L-x)$

Separating variables and integrating: $y = \frac{Fx^2}{6EI} (3L-x)$

$$y_{x=L} = \frac{FL^3}{3EI}$$



$$\kappa = \frac{d\theta}{ds} = \frac{M}{EI}$$

Curvature proportional to moment

Linear beam theory

PRECISION POINT

TO THE POINT PRECISION ENGINEERING KNOWLEDGE DATABASE



Practical



Free



Concise

Search Precision Point database...

Beam theory: Tension/compression and shear

Beam theory: Bending

Beam theory: Torsion

Beam theory: Buckling

Beam theory: Stiffness of combined loads

Torsion of leaf springs: Restrained warping

Buckling fundamentals

Buckling phenomena

Area moment of inertia

Mass moment of inertia

Positioning terminology

Hertz contact: Universal point

Body: m, C_G

Pre-A (10^{-1})

Load case	Condition	Curvature θ Slope δy	Reaction force R Shear force D Reaction moment M_R	Status of Stiffness C
	$\theta_A = 0$	$\theta_B = \frac{FL}{2EI}$ $\delta y_B = -\frac{FL^2(3L-z)}{12EI}$ $\delta y_{max} = -\frac{FL^3}{6EI} @ z = L$	$R_A = F$ $R_B = N.A.$ $D_1 = F$ $M_{Rz} = F(z-L)$ $M_{Rmax} = -FL @ z = 0$	$ r_z = \frac{FL^3}{6EI} @ z = -\frac{FL^3}{6EI}$ $ r_{max} = \frac{FL^3}{6EI} @ z = 0$ $ K_z = \left \frac{d^2}{dz^2} \right = \frac{FL}{EI} @ z = L$
	$\theta_A = 0$	$\theta_B = \frac{FL}{2EI}$ $\delta y_B = -\frac{FL^2}{2EI}$ $\delta y_{max} = -\frac{3FL^2}{8EI} @ z = L$	$R_A = 0$ $R_B = N.A.$ $D_1 = N.A.$ $M_{Rz} = M$ $M_{Rmax} = M @ z = const.$	$ r_z = \frac{FL^3}{6EI} @ z = \frac{FL^3}{6EI}$ $ r_{max} = \frac{3FL^3}{8EI} @ z = const.$ $ K_z = \left \frac{d^2}{dz^2} \right = \frac{FL}{EI} @ z = L$
	$\theta_A = 0$	$\theta_B = \frac{qL^2}{2EI}$ $\delta y_B = -\frac{qL^3(3L-z)}{6EI}$ $\delta y_{max} = -\frac{qL^4}{8EI} @ z = L$	$R_A = qL$ $R_B = N.A.$ $D_1 = q(L-z)$ $M_{Rz} = -\frac{qz^2}{2}$ $M_{Rmax} = -\frac{qL^2}{8} @ z = 0$	$ r_z = \frac{qL^4}{8EI} @ z = -\frac{3qL^4}{8EI}$ $ r_{max} = \frac{qL^4}{8EI} @ z = 0$ $ K_z = \left \frac{d^2}{dz^2} \right = \frac{qL}{EI} @ z = L$
	$0 \leq z \leq a$	$\theta_A = \frac{Fz(L-z)}{2EI}$ $\theta_B = \frac{Fz(L-z)}{2EI}$	$R_A = \frac{Fz}{L}$ $R_B = \frac{Fz}{L}$ $D_1 = -Fz$	$ r_z = \frac{Fz^3}{6EI} @ z = \frac{Fz^3}{6EI}$ $ r_{max} = \frac{Fz^3}{6EI} @ z = a$

12

$\theta_A = 0$

$\theta_B = 0$

$\delta y_z = -\frac{Fz^2(3L-2z)}{12EI}$

$\delta y_{max} = -\frac{FL^3}{12EI} @ z = L$

$R_A = F$

$R_B = 0$

$D_z = F$

$M_{Rz} = \frac{FL-2Fz}{2}$

$M_{Rmax} = \frac{FL-2Fz}{2} \text{ resp. } -\frac{FL}{2}$
 $@ z = 0 \text{ resp. } L$

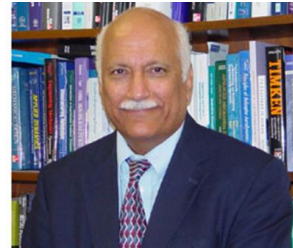
$|\sigma_z| = \frac{|M_{Rz}|}{I_x} u = \frac{|u(FL-2Fz)|}{2I_x}$

$|\sigma_{max}| = \frac{|F|Lu}{2I_x} @ \frac{z=0}{z=L}$

$|C_y| = \left| \frac{F}{\delta y_{max}} \right| = \frac{12EI_x}{L^3} @ z = L$

	$\theta_A = \frac{qL^2}{2EI}$ $\theta_B = \frac{qL^2}{2EI}$ $\delta y_B = -\frac{qL^3}{6EI} \left[\frac{1}{2} - 2(z) + (z)^2 \right]$ $\delta y_{max} = -\frac{qL^4}{8EI} @ z = \frac{L}{2}$	$M_{Rmax} = M @ z = L$ $R_A = \frac{qL}{2}$ $R_B = \frac{qL}{2}$ $D_1 = \frac{qL}{2} - qz$ $M_{Rz} = \frac{qz^2}{2}$	$ r_z = \frac{qL^4}{8EI} @ z = -\frac{3qL^4}{8EI}$ $ r_{max} = \frac{qL^4}{8EI} @ z = \frac{L}{2}$ $ K_z = \left \frac{d^2}{dz^2} \right = \frac{qL}{EI} @ z = \frac{L}{2}$
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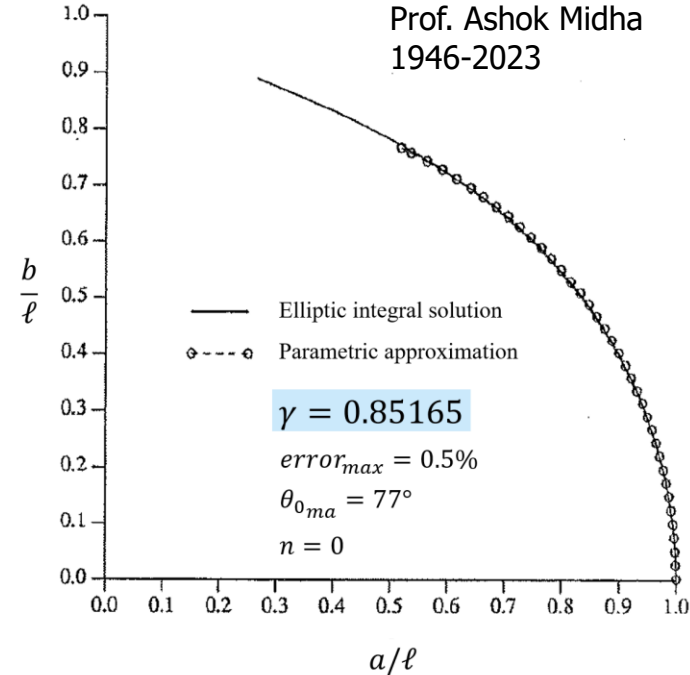
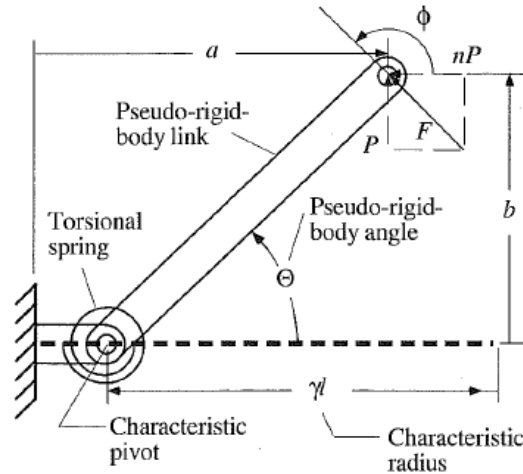
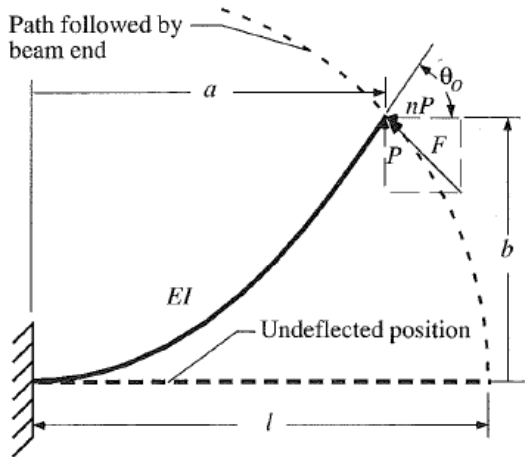
Large deflections



Prof. Ashok Midha
1946-2023

Elliptic integral of $M = EI \frac{d\theta}{ds}$ is cumbersome...

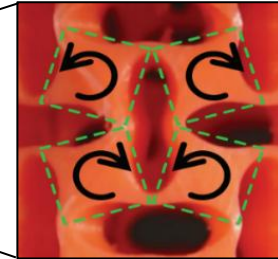
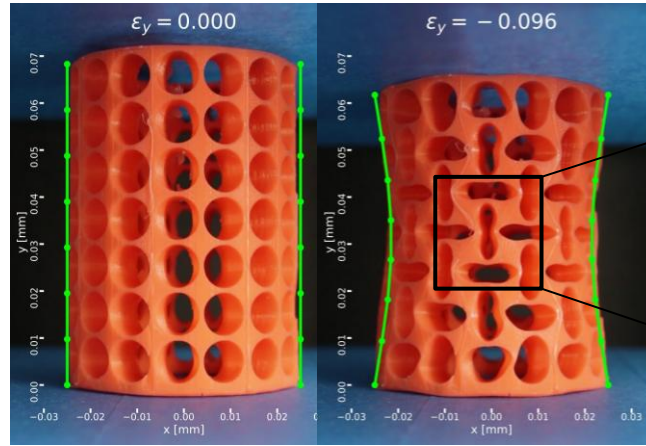
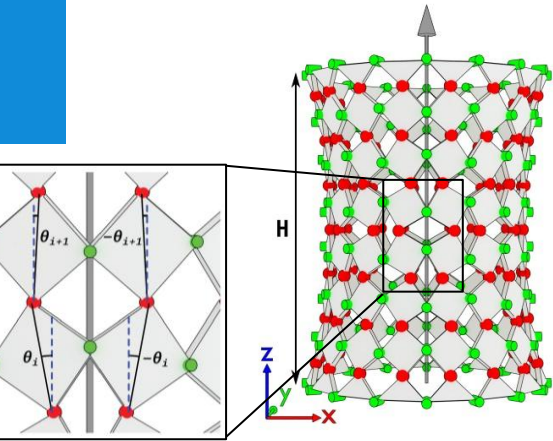
Approximation by arc motion and torsional spring:
Pseudo-Rigid-Body Model (PRBM, Midha and Howell)





Freek Broeren

Spatial kinematic modelling

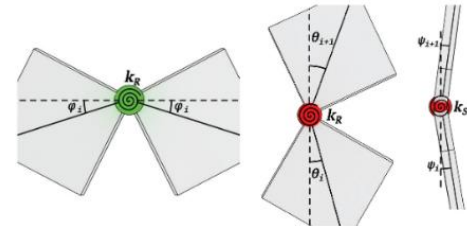
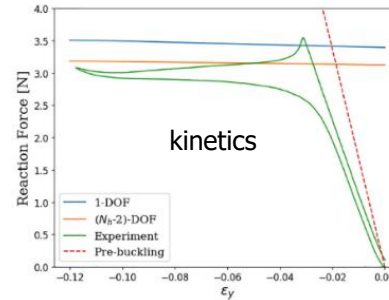
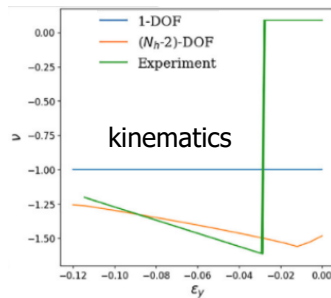


$$r_i = \frac{l \cos(\theta_i)}{2 \sin\left(\frac{\pi}{N_c}\right)}$$

$$h_i = l \cos(\theta_i) \cos(\psi_i)$$

$$H = \frac{h_0 + h_{N_h}}{2} + \sum_{i=2}^{N_h-1} h_i$$

$$\nu = -\frac{H}{r} \frac{\partial r}{\partial H} = -1$$



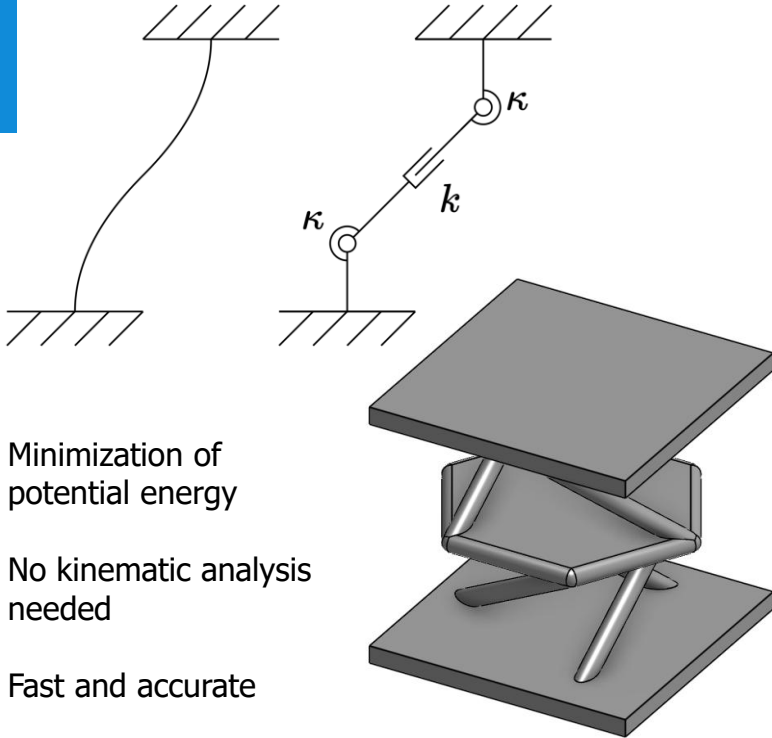
$$E = E_h + E_v + E_s$$

$$= \frac{1}{2} N_c k_R \left(N_h (2\phi(\theta))^2 + (N_h - 1) (2\theta)^2 \right)$$



Domas Syaifoel

Energy method (pyBRM)



Minimization of potential energy

No kinematic analysis needed

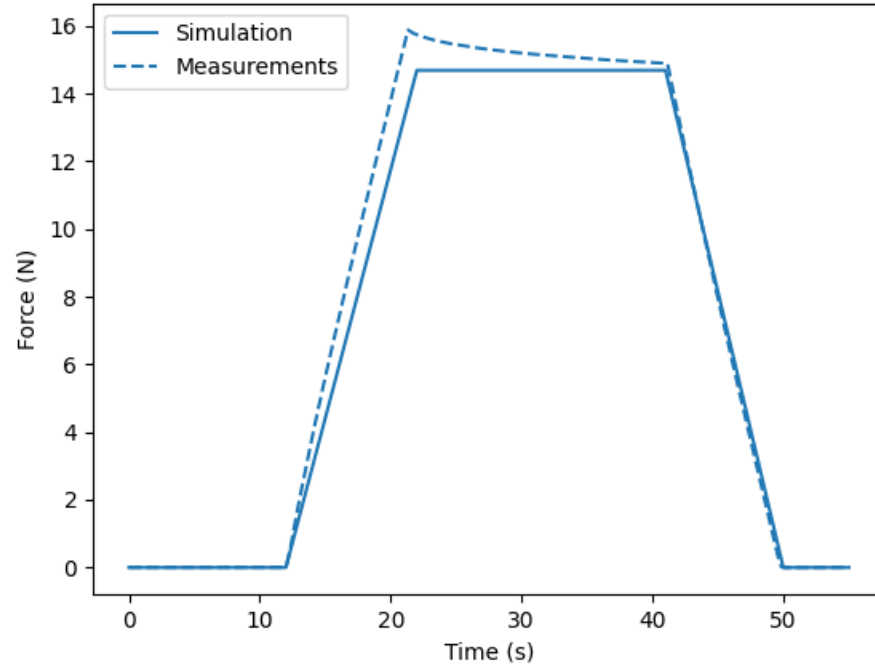
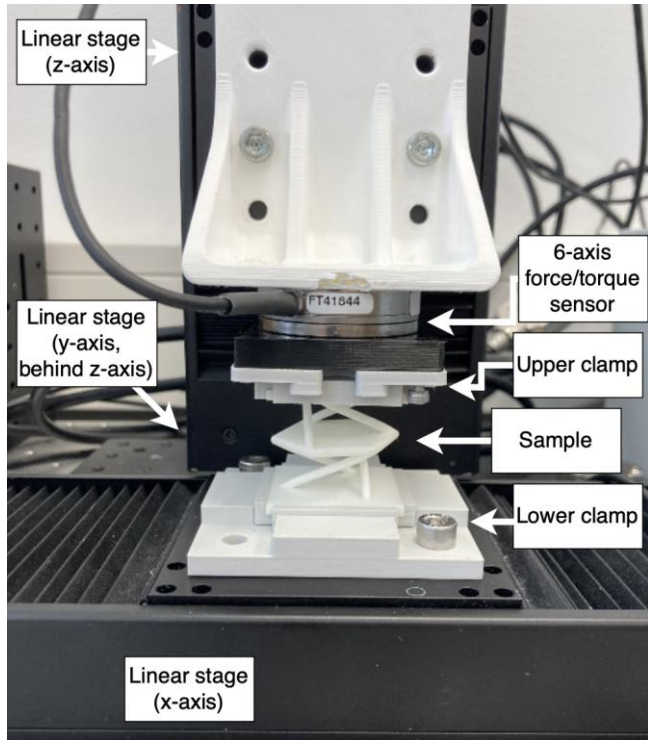
Fast and accurate

```
1 p = PRBM(3)
2
3 p.add_body('A', (0, 0, 0))
4 p.add_body('B', (0, 0, 15*mm))
5 p.add_body('C', (0, 0, 3*cm))
6
7 t = mm
8 A = pi*t**2
9 E = 1650e6
10 I = pi*t**4/2
11
12 n = 3
13 r = 14*mm
14
15 for i in range(n):
16     p.add_flexure('A', (r*cos(i/n*2*pi), r*sin(i/n*2*pi), 0),
17                  'B', (r*cos((i + 1)/n*2*pi), r*sin((i + 1)/n*2*pi), 0))
18     p.add_flexure('C', (r*cos((i - .5)/n*2*pi), r*sin((i - .5)/n*2*pi), 0),
19                  'B', (r*cos((i + .5)/n*2*pi), r*sin((i + .5)/n*2*pi), 0))
20
21 p.show()
```

Energy method (pyBRM)



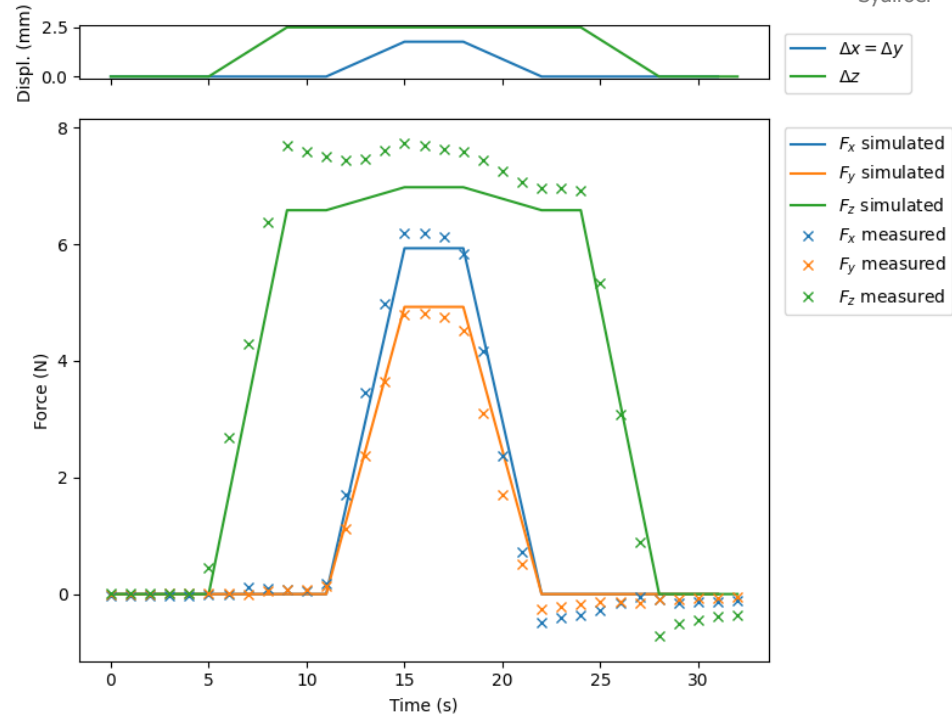
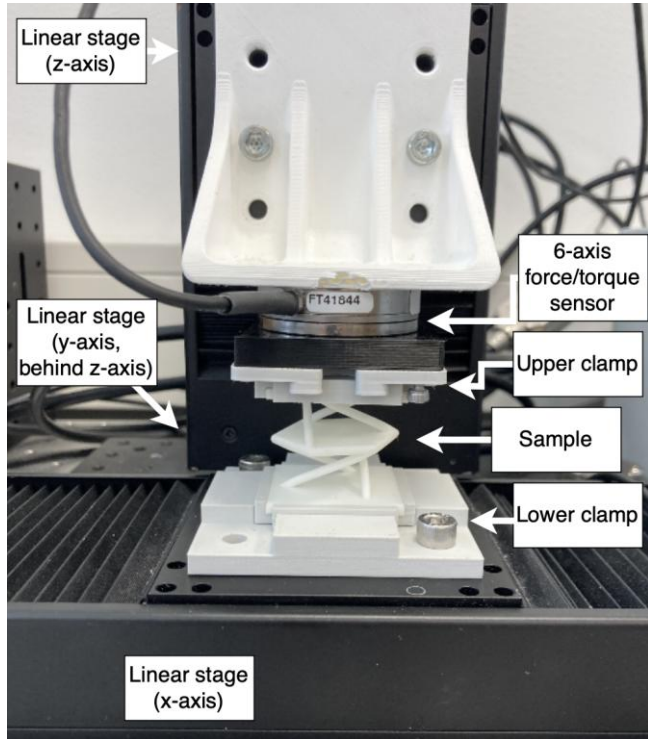
Domas Syaifoel



Energy method (pyBRM)



Domas Syaifoel



Precision Compliant Mechanisms

Just Herder

Characteristics of compliant mechanisms

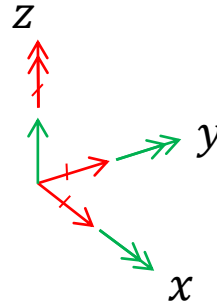
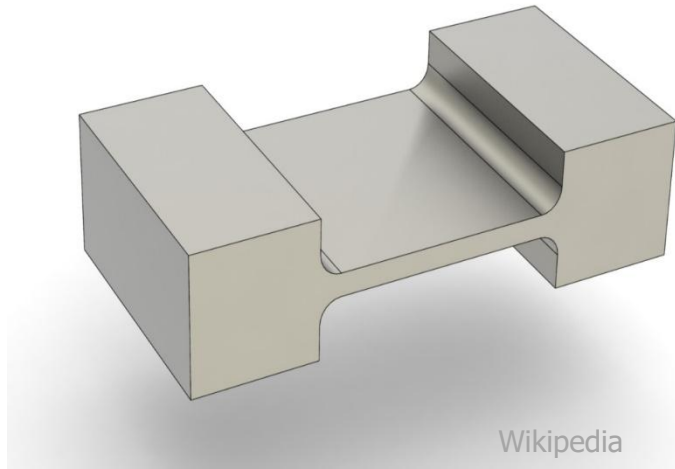
Well-behaved flexures

Strategies to improve behavior

Static balancing

Trends and prospects

Flexure as a revolute joint

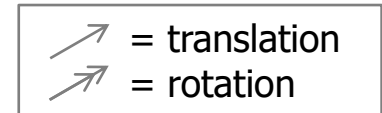
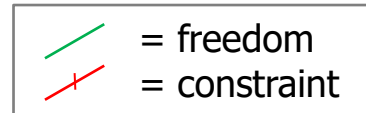


'Good' flexure:

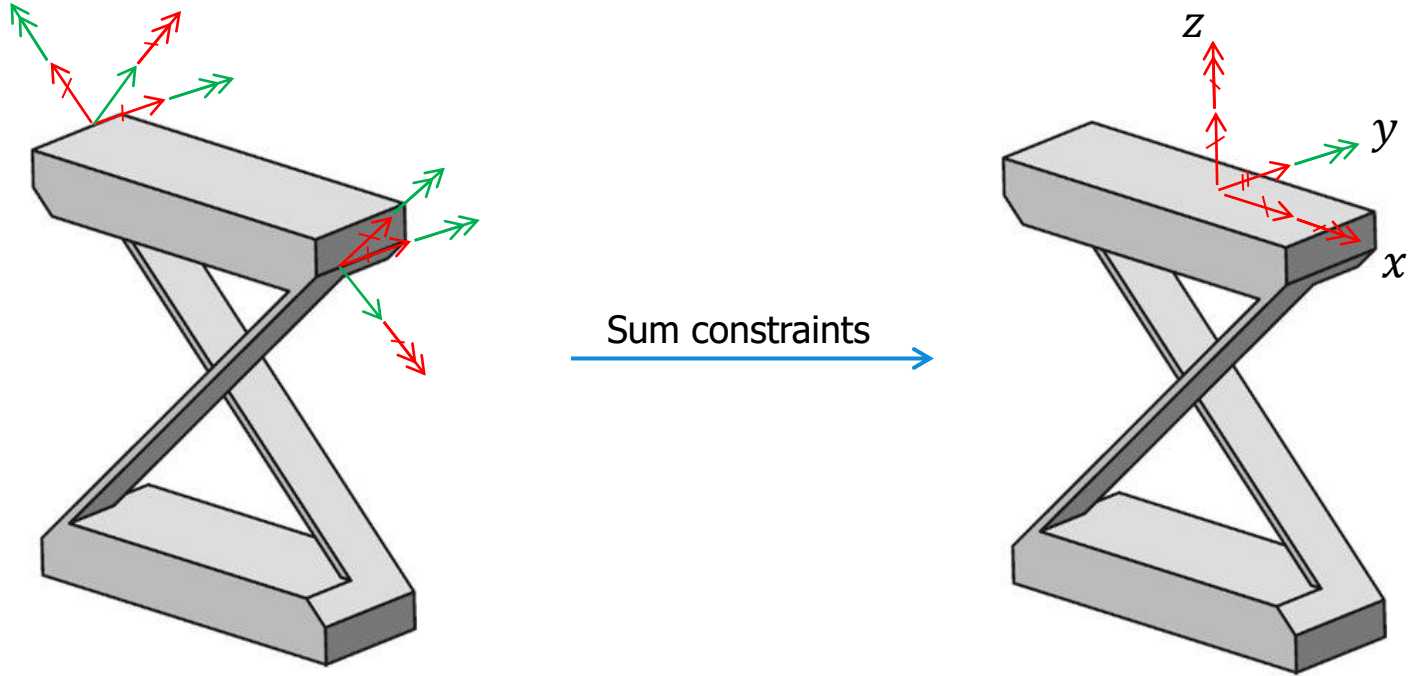
$$\frac{k_f}{k_c} \gg 150$$

$$\frac{k_{c,max}}{k_{c,min}} \ll 50$$

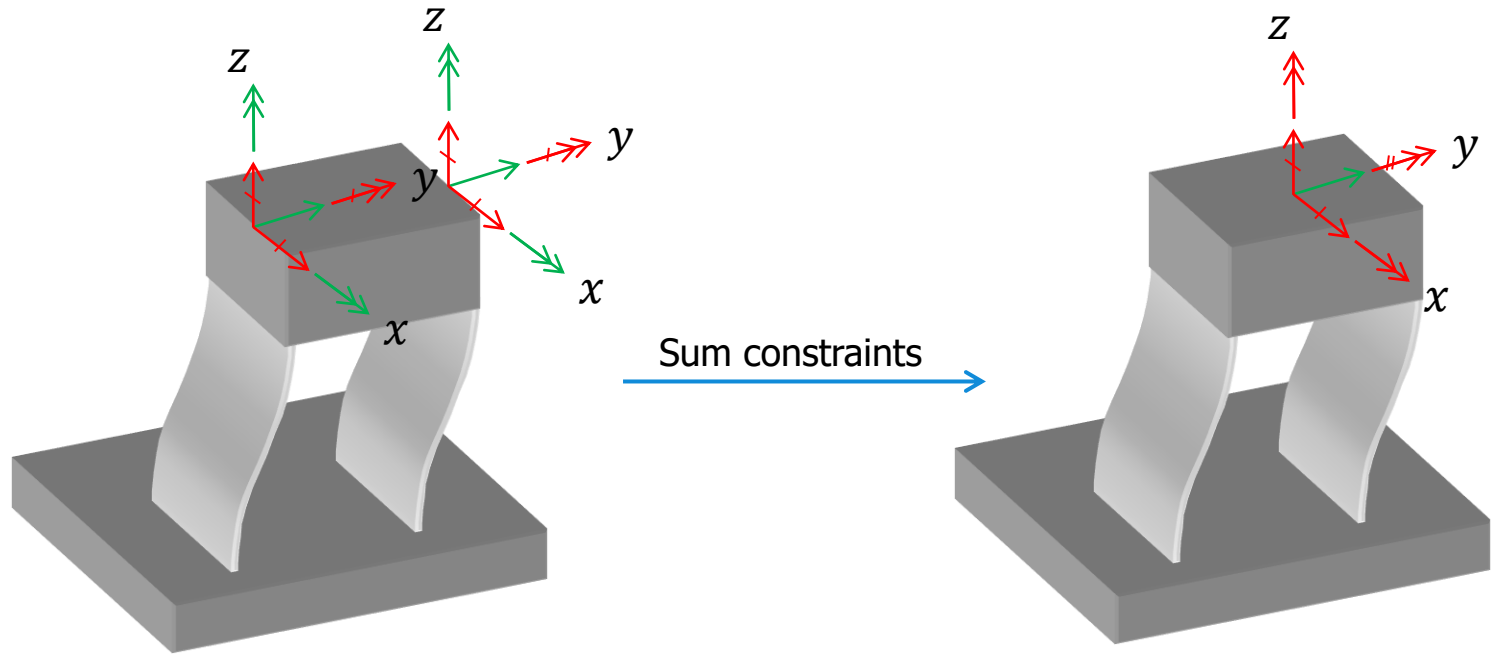
k_f = freedom stiffness, DoF
 k_c = constraint stiffness, DoC



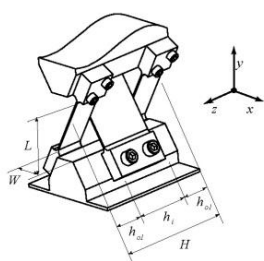
Cross-flexure as a better revolute joint



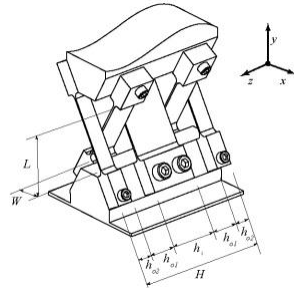
Double flexure prismatic joint



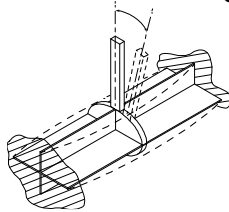
Problem: stiffness decay at deflection



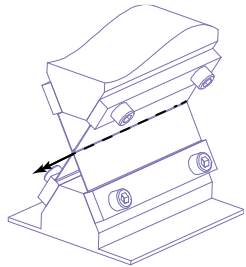
Three flexure cross hinge



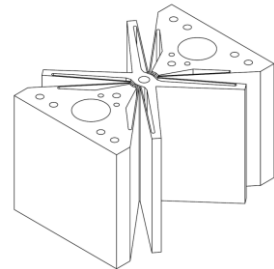
Five flexure cross hinge



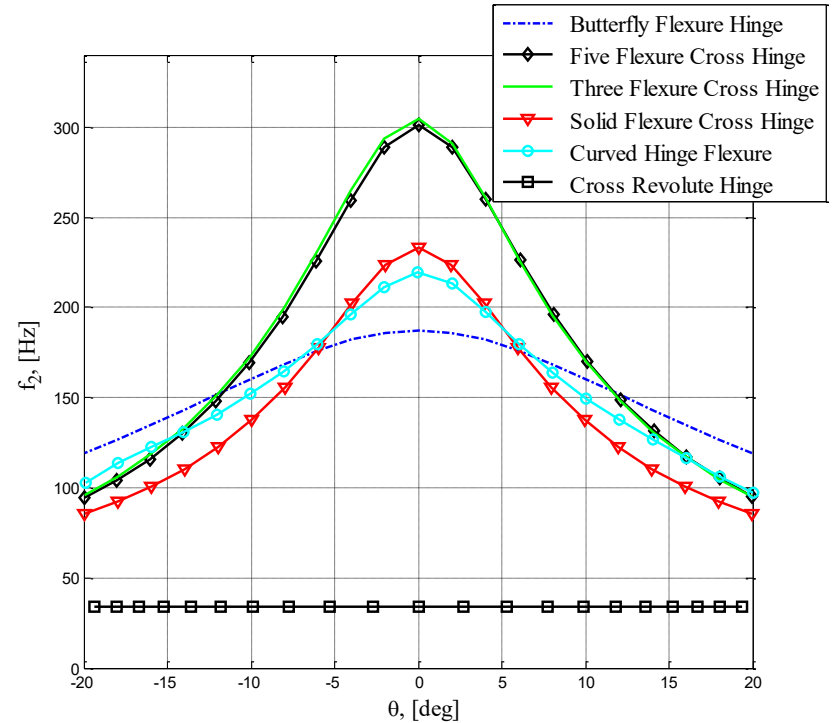
Cross Revolute hinge



Solid flexure cross hinge

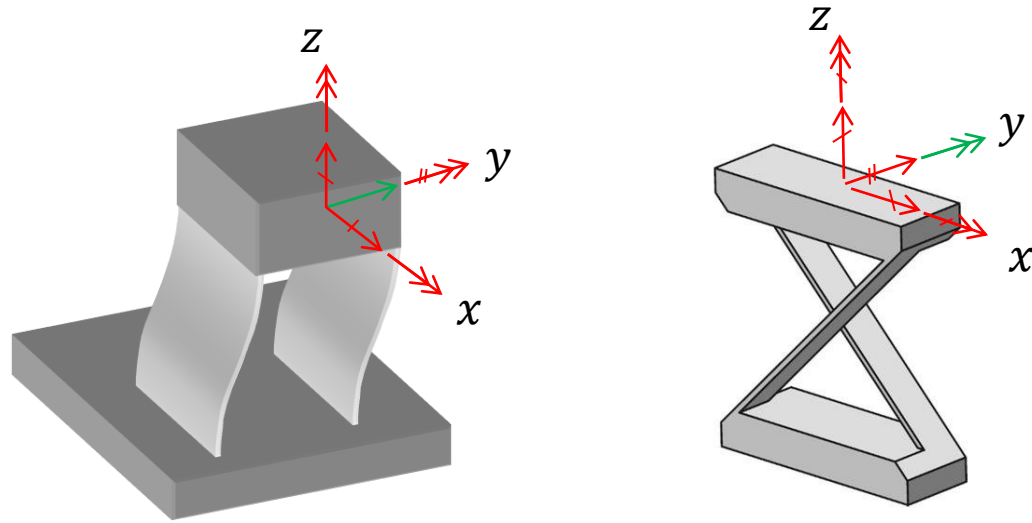


Butterfly flexure hinge



What makes a good compliant joint

Degrees of freedom (green): low freedom stiffness k_f } High stiffness ratio $\frac{k_c}{k_f}$
Constraint directions (red): high constraint stiffness k_c



Torsion reinforcement

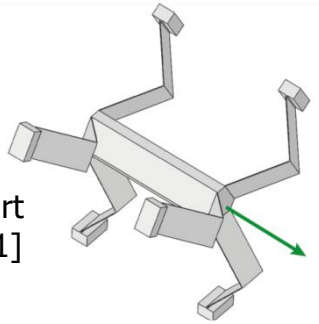
Increase range of motion:

- Series-parallel
- Initial stress or curve

Increase stiffness ratio:

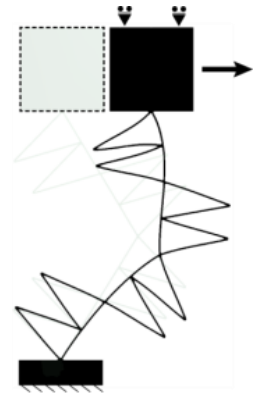
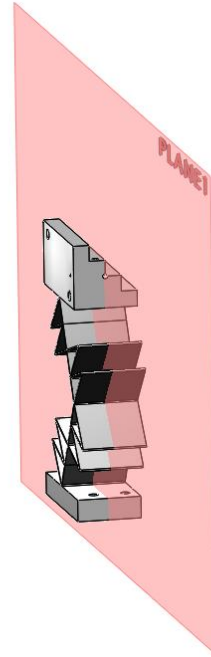
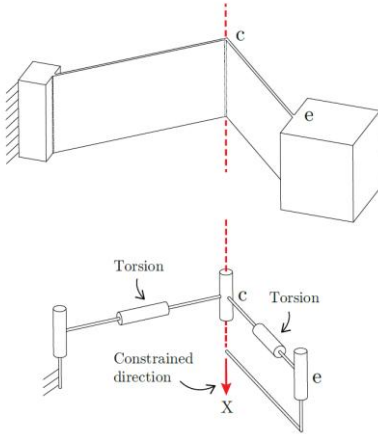
- Reduce k_f : static balance
- **Increase k_c : reinforcement**

Reinforcement



State-of-the-art linear guide [1]

Based on 6 folded flexures:

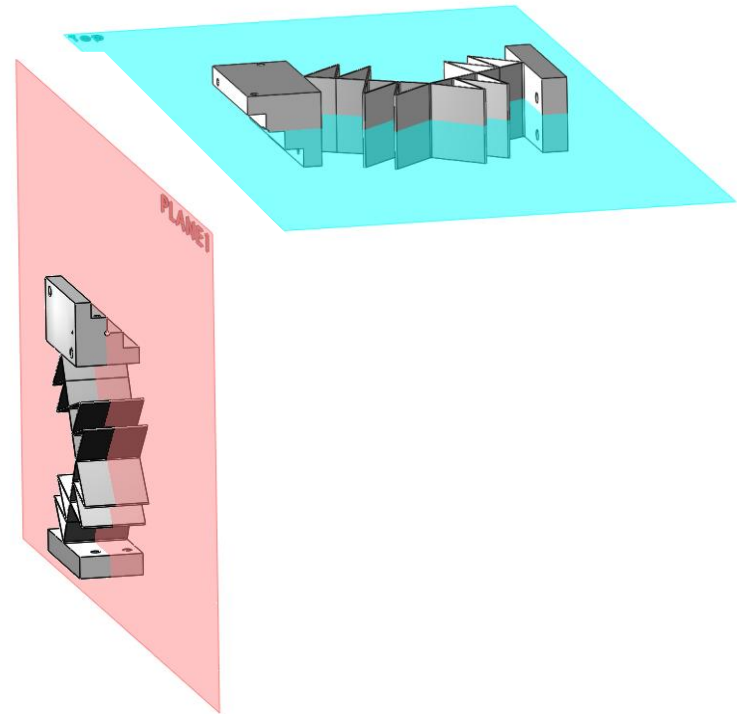


Distributed compliance

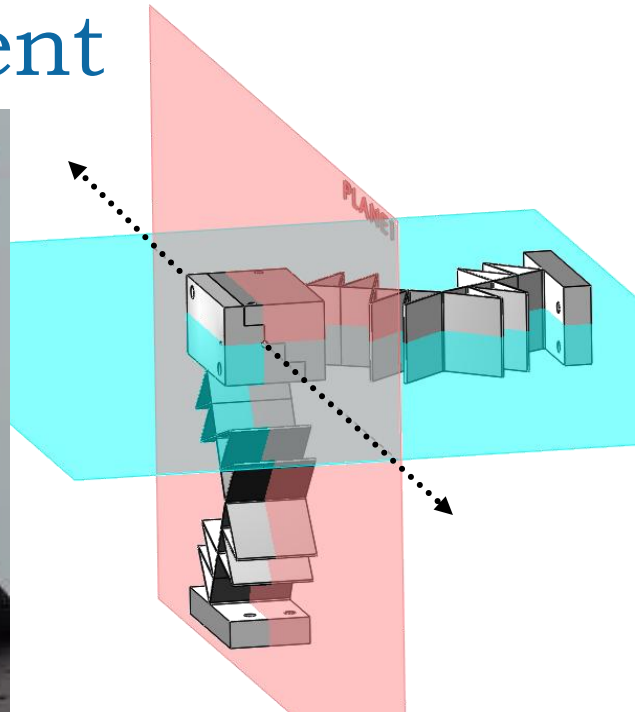
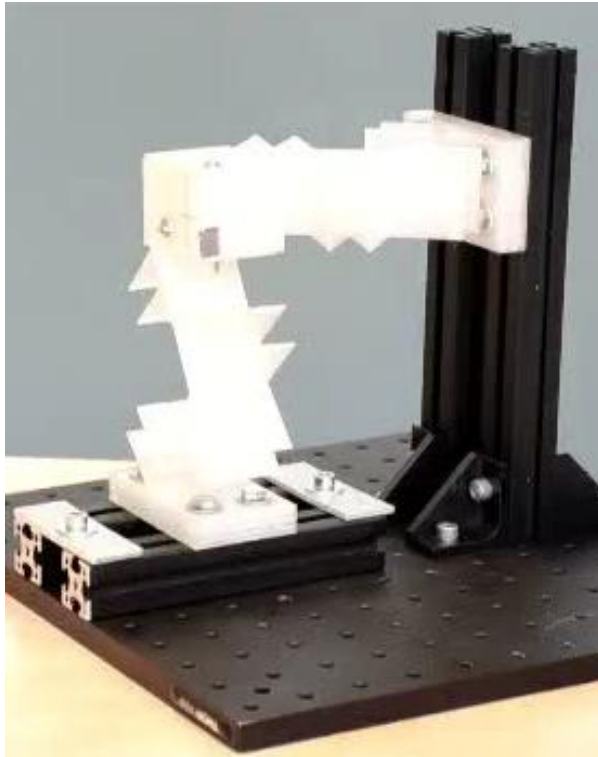
Jelle Rommers



Reinforcement



Reinforcement



Advantages

- Less obstructive build volume
- Fewer elements
- Higher support stiffness

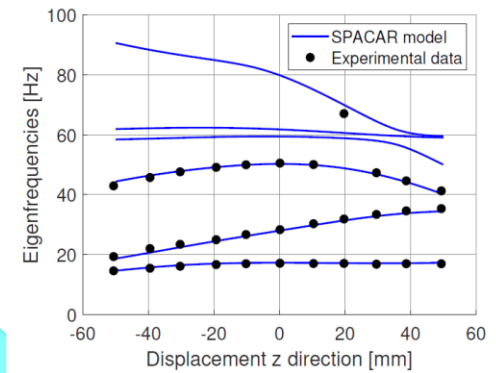
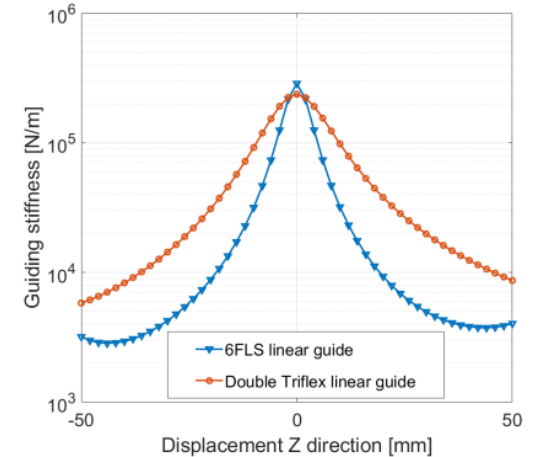
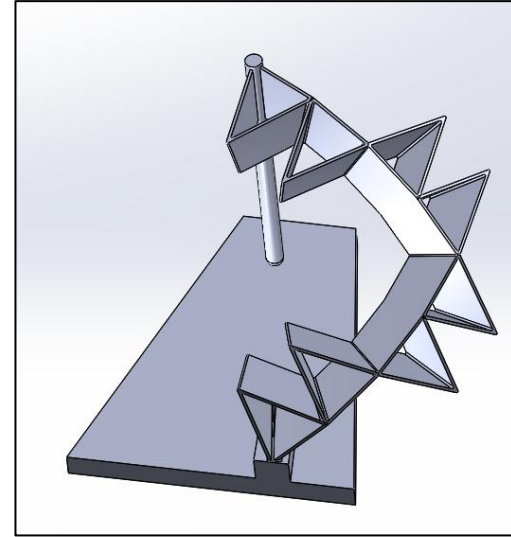
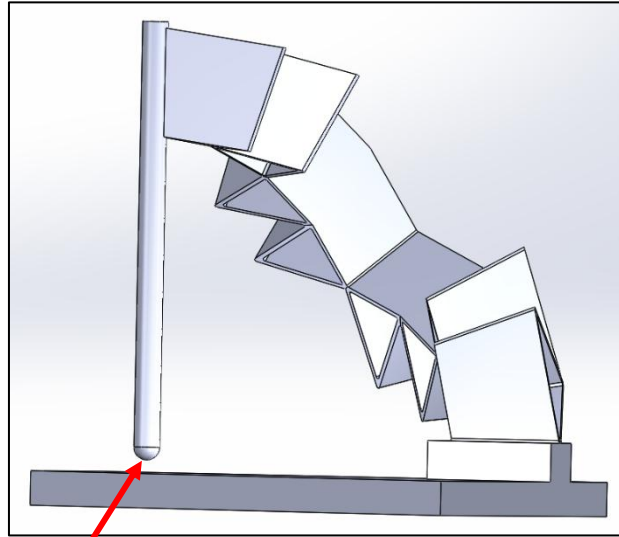
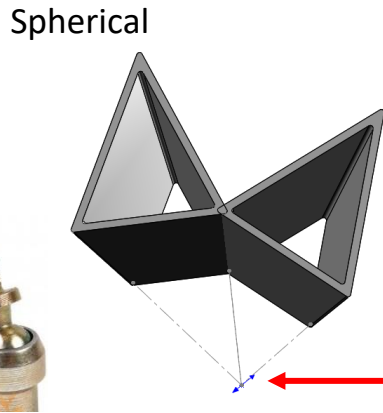


Fig. 15: Measured and modelled parasitic eigenfrequencies of the Nylon prototype of the 2-TR-FLS design. The eigenfrequency in motion direction (not displayed) is 2.1 Hz.

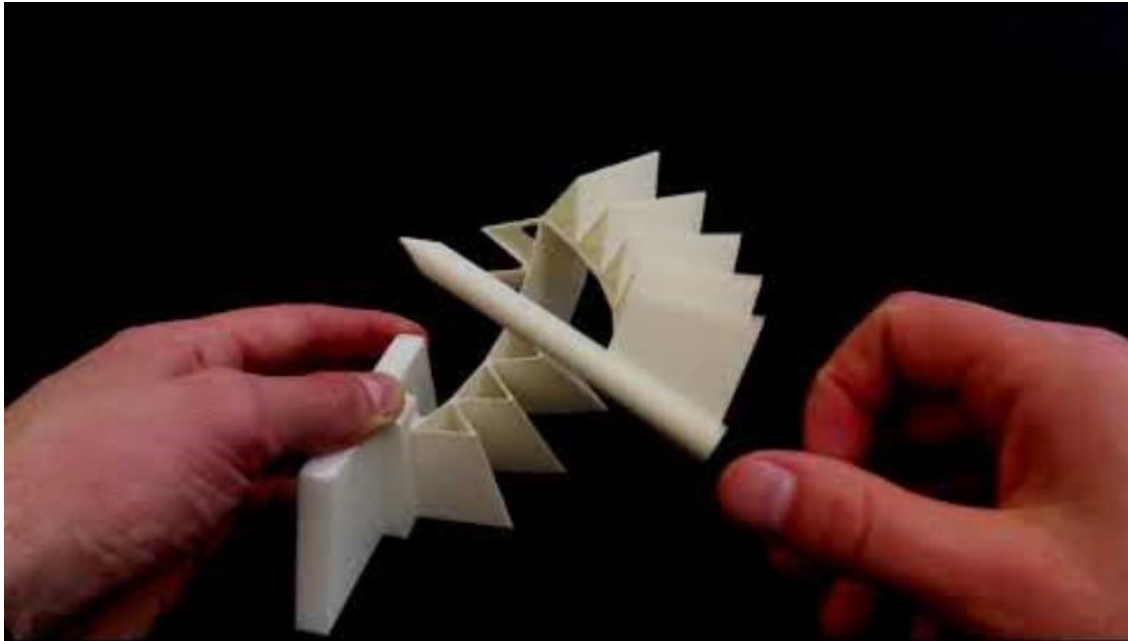


Reinforcement



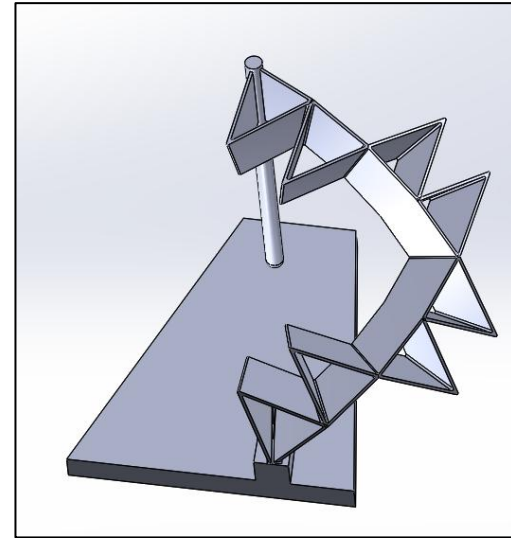
Remote center of rotation

Reinforcement

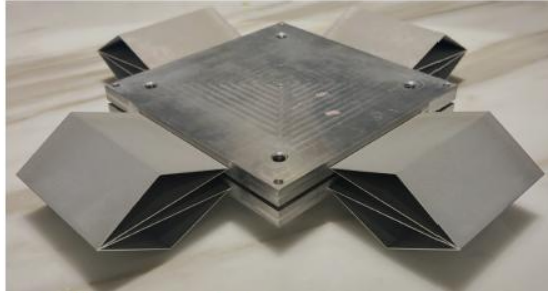


<https://www.youtube.com/watch?v=DAngcygU7tc>

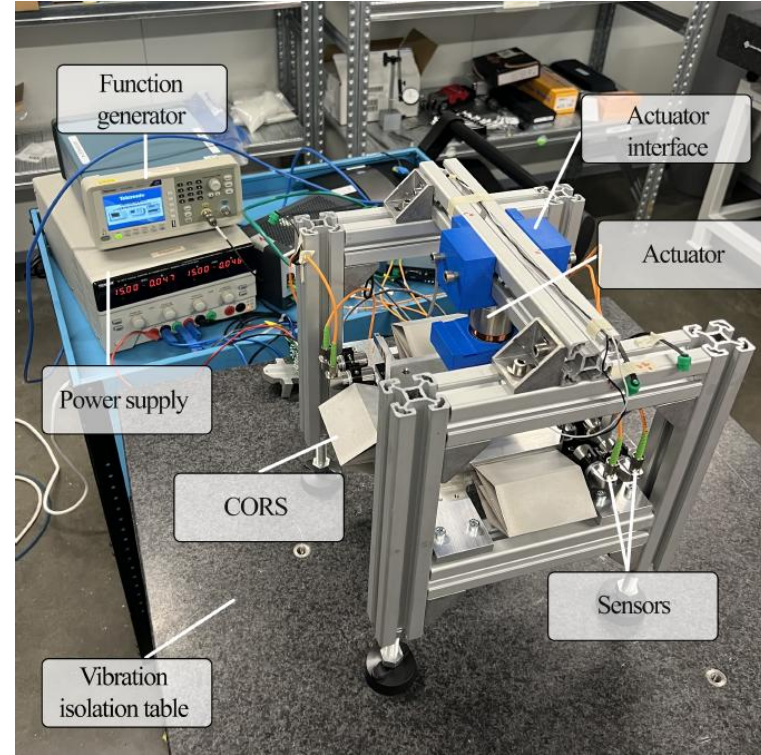
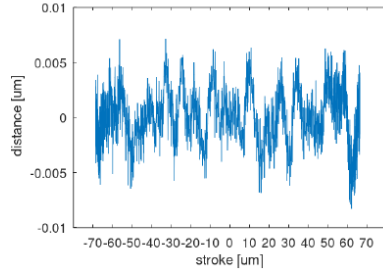
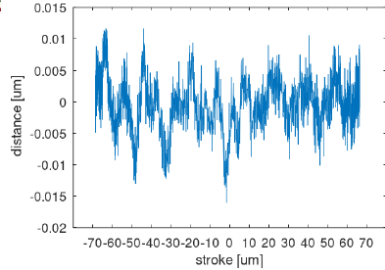
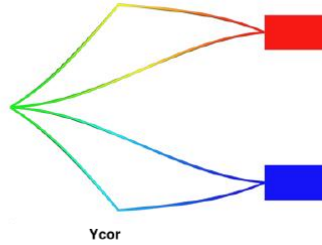
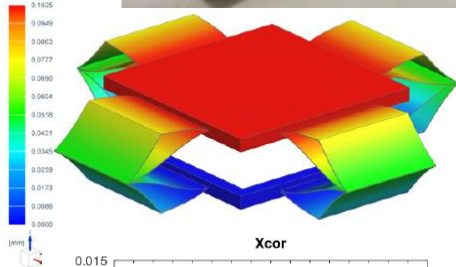
390k views



Reinforced compliant Sarrus mech.



0.7 nm/ μm
5 nm over 140 μm
total stroke of 5 mm



Initial stress or curve

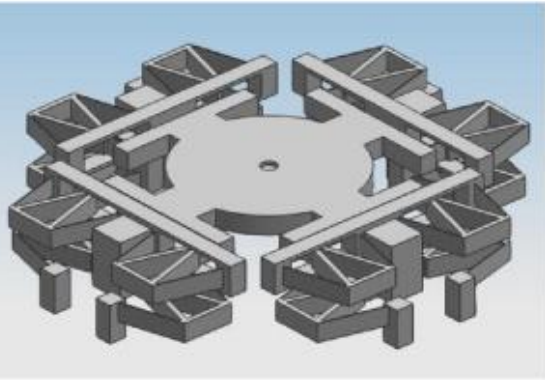
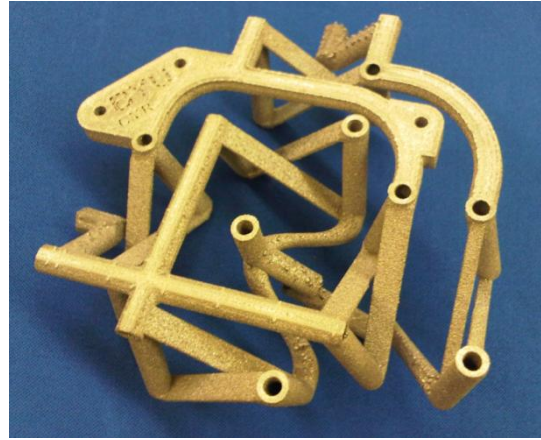
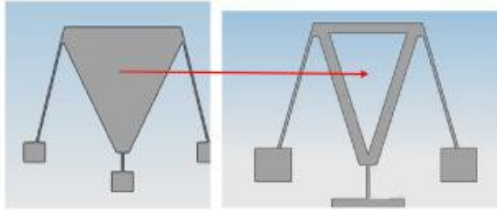
Increase range of motion:

- Series-parallel
- **Initial stress or curve**

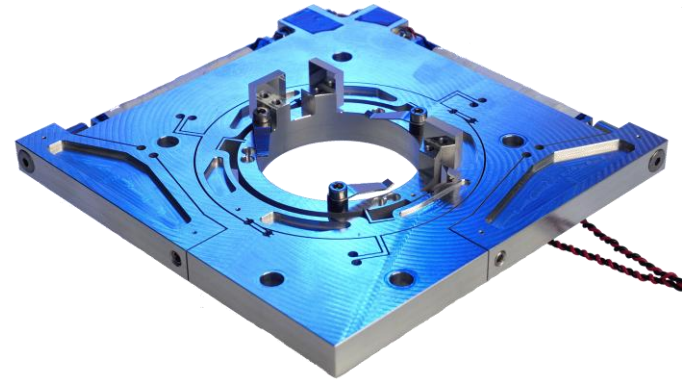
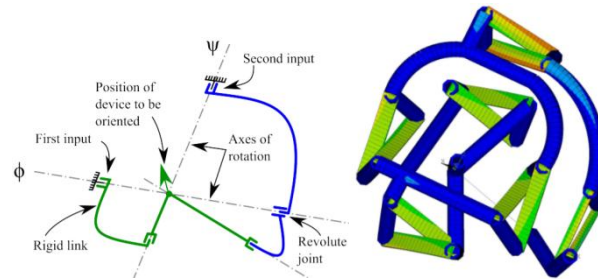
Increase stiffness ratio:


- Reduce k_f : static balance
- Increase k_c : reinforcement

Modern compliant mechanisms

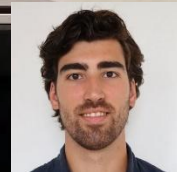


S Wan, Q Xu, Design and analysis of a new compliant XY micropositioning stage based on Roberts mechanism, *Mech. Mach. Theory*, 2016





Optimized for:
Straight-line motion
Constant support stiffness
Second modal frequency



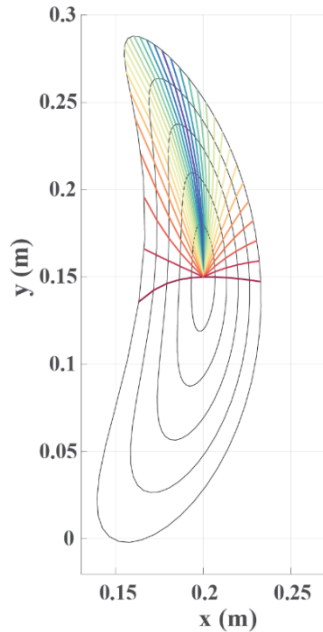
Flip Colin

Curved with symmetric stiffness

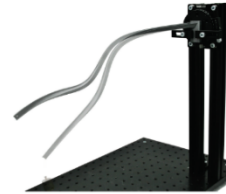
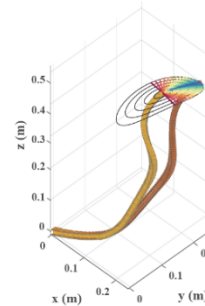
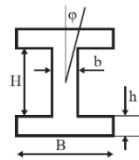
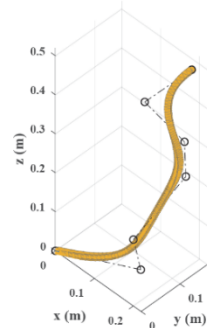


Ali Amoozandeh

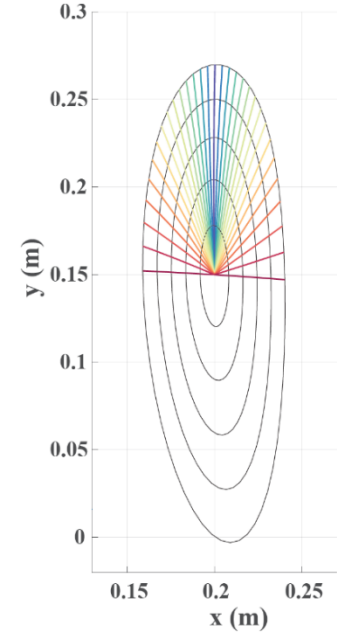
Typical asymmetric behavior



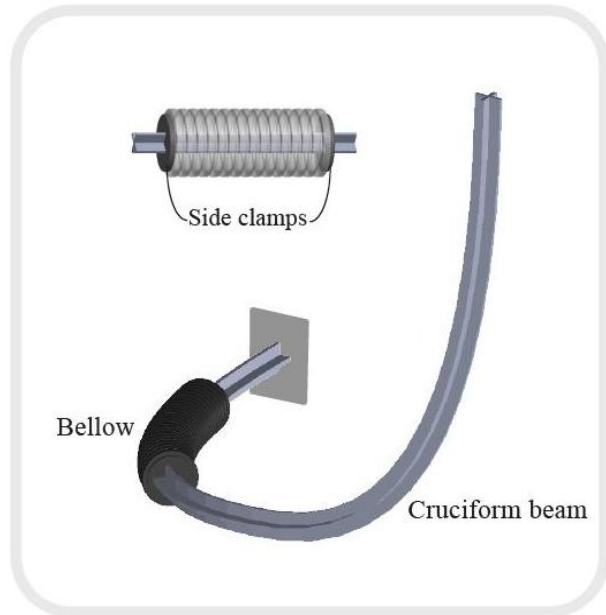
Optimizing section and shape



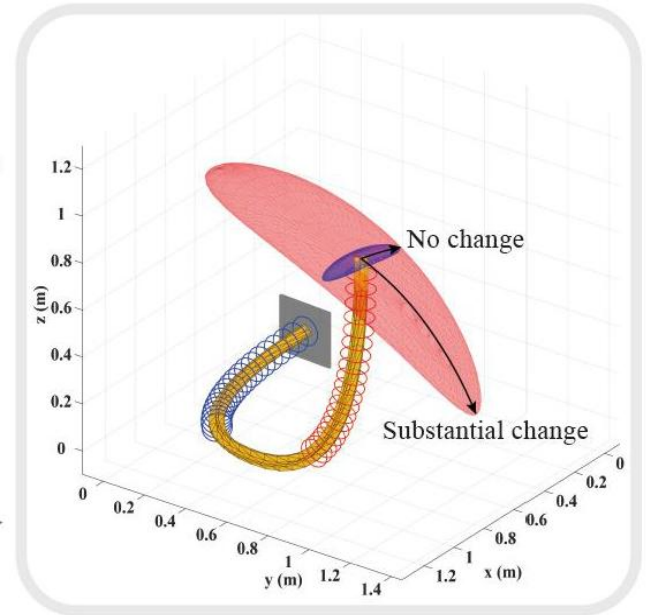
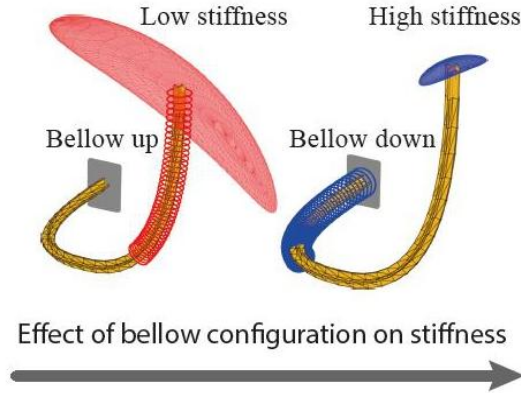
Corrected symmetric behavior



Anisotropically adaptive



Bellow acts as a sliding torsional stiffener

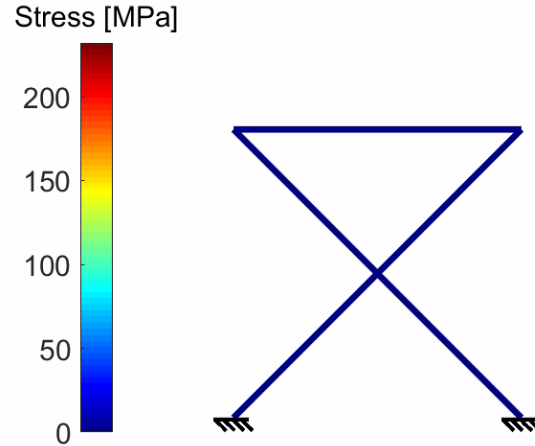
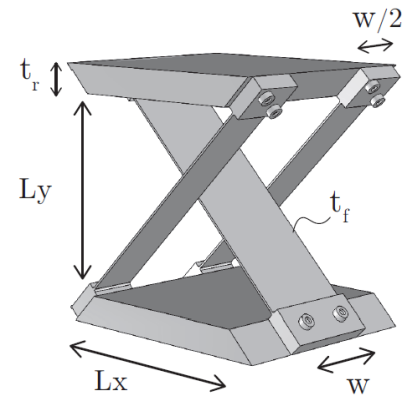


Anisotropically adaptive stiffness

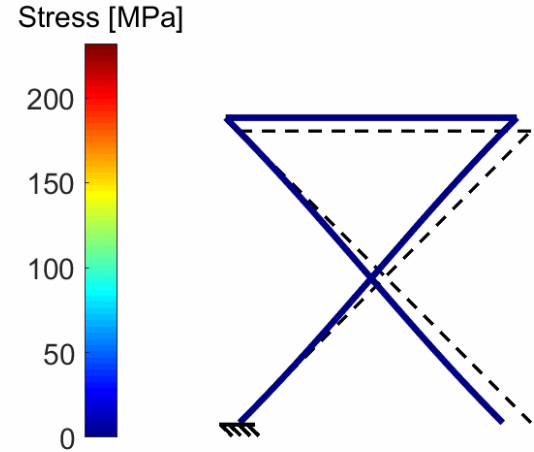
Stress and Geometry (STAGE)



Jelle Rommers



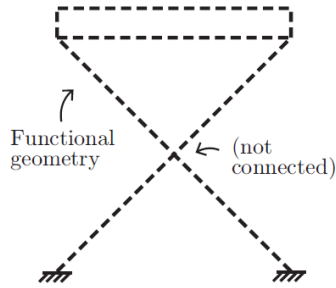
Conventional design:
Initial state is stress-free,
High stress in extreme poses.
Max stress asymmetric.



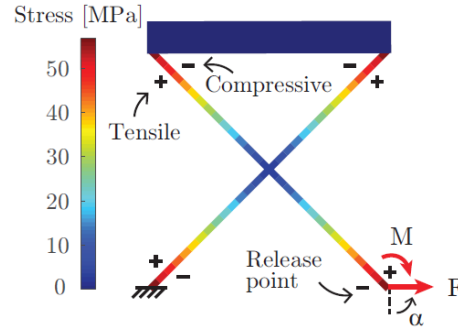
Pre-stressed design:
Fabrication shape is stress-free,
initial state is pre-stressed.
Reduced stress in extreme poses.

Stress and Geometry (STAGE)

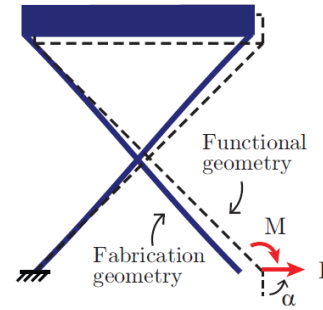
Jelle
Rommers



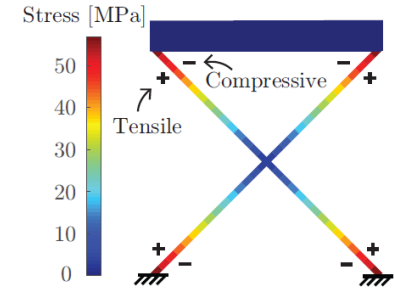
Step 1 Design of the functional geometry



Step 2 Design of the internal stress distribution by loading a release point

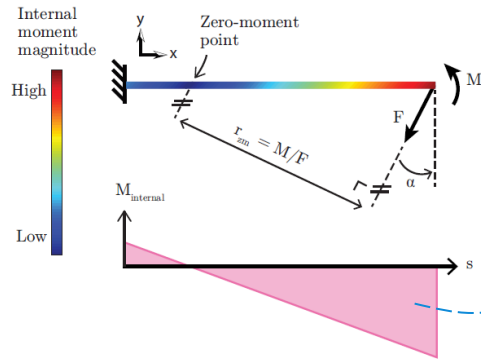


Step 3 Calculation by inverse FEM of the stress-free geometry for manufacturing



Step 4 Assembly to obtain the functional geometry with the desired initial stress

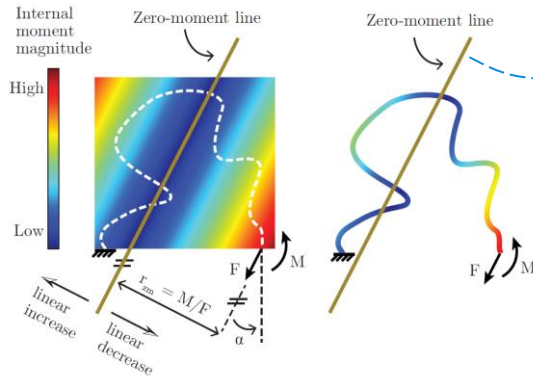
Initial stress or curve



Stress dominated by bending: $\sigma = M_i \frac{t_f}{2I}$

Stress proportional with internal moment, use this to visualize internal stress:

$$M_i(s) = \cos(\alpha)F(L - s) - M$$



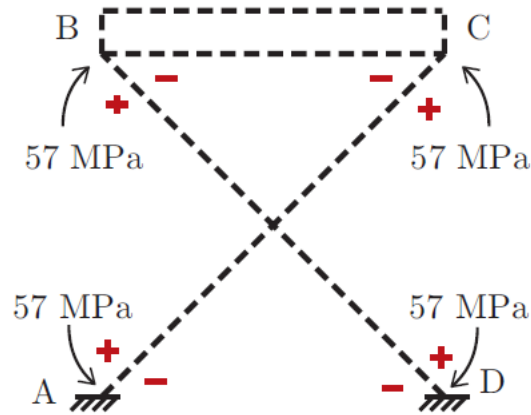
From this, the zero-moment line (ZML) can be derived:

$$M_i(r) = Fr - M$$

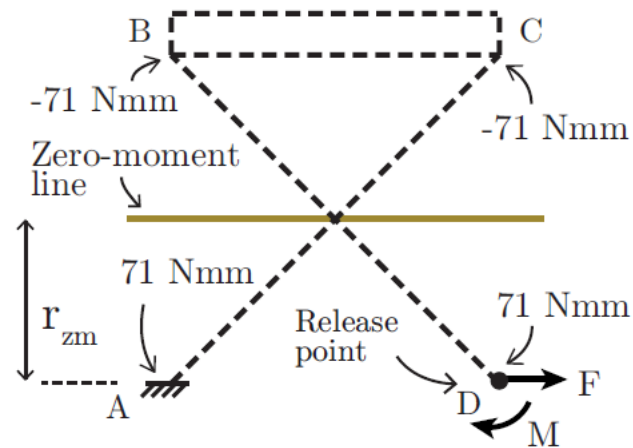
Design of stress distribution:

- ZML parallel to external force F
- Distance ZML to action line F is: $r_z = M/F$
- Gradient M -field (perp to ZML) equal to $|F|$

Stress and Geometry (STAGE)



Desired designed stress field



Corresponding load field

Initial stress or curve

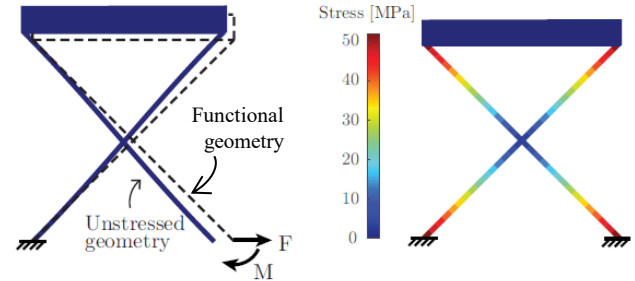
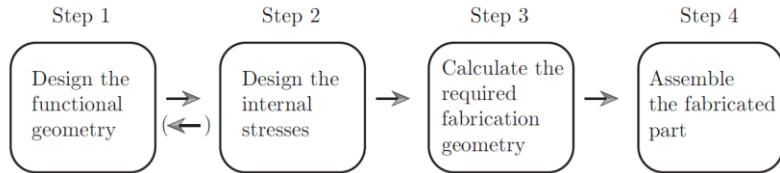
Procedure:

Step 1: Design the functional geometry as in a conventional way

Step 2: Design the initial stress configuration

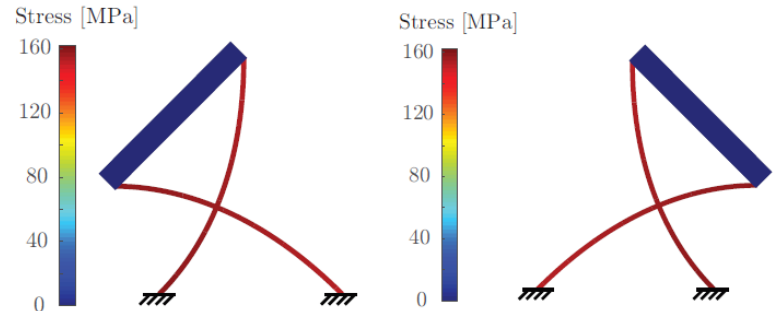
Step 3: Calculate the required fabrication geometry (optim or iFEM)

Step 4: Assemble the fabricated part in the initially designed geometry



(a) As fabricated.

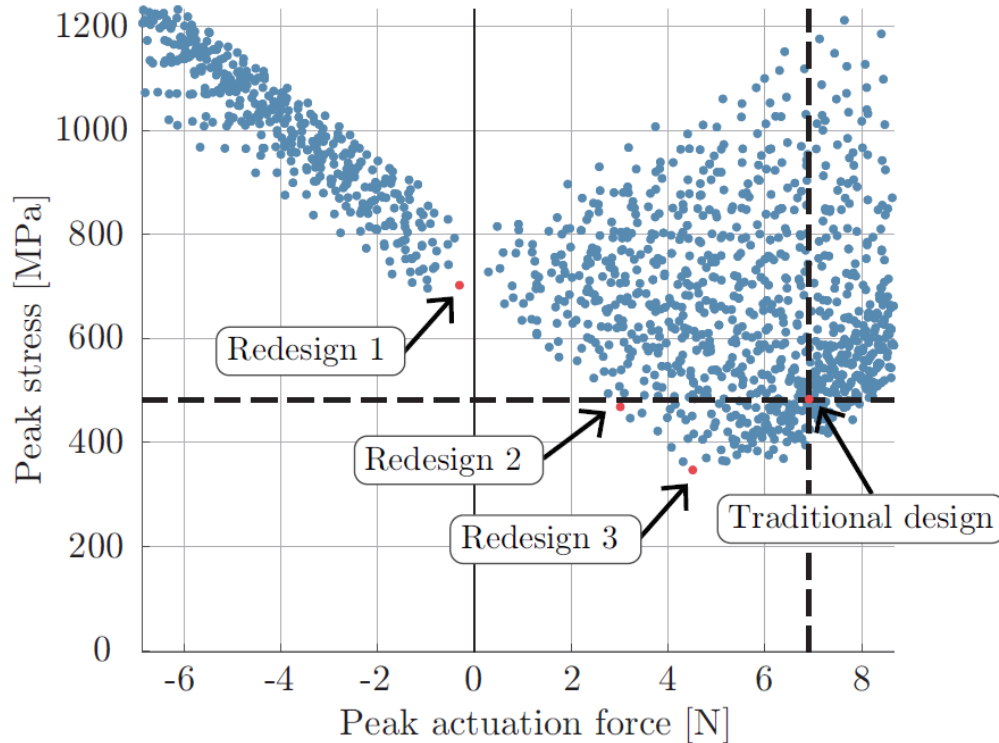
(b) Assembled.



(c) After +45 degrees rotation.

(d) After -45 degrees rotation.

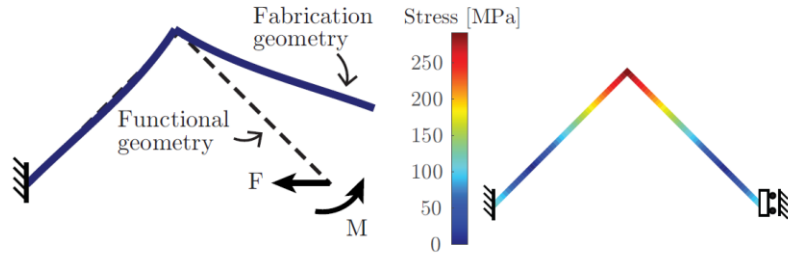
Initial stress or curve



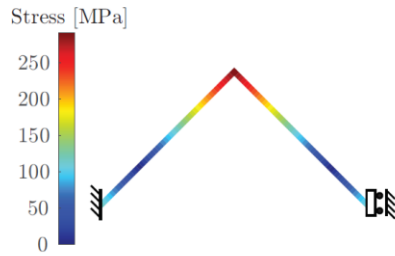
Any closed-loop flexure can be optimized by initial stress:

- Reduced motion stiffness
- Reduced maximum stress
- Both

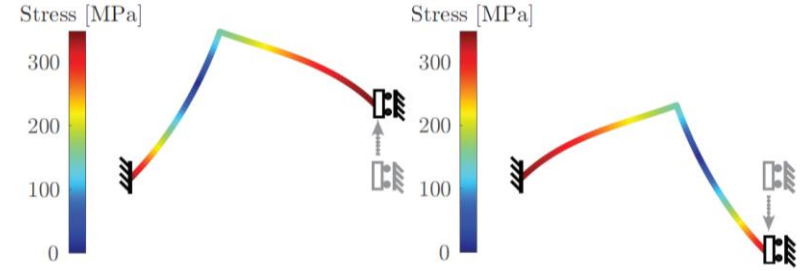
Initial stress or curve



(a) As fabricated.

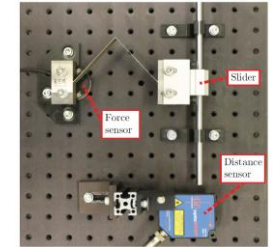
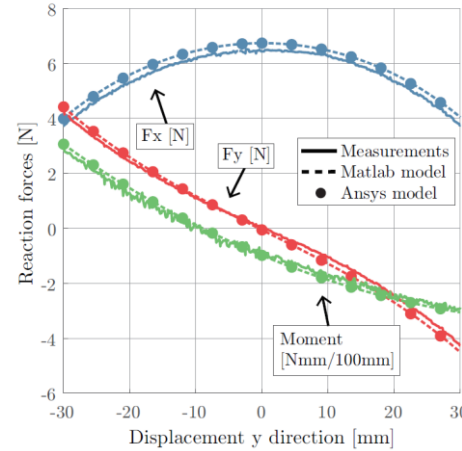
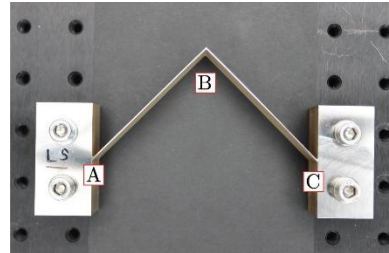
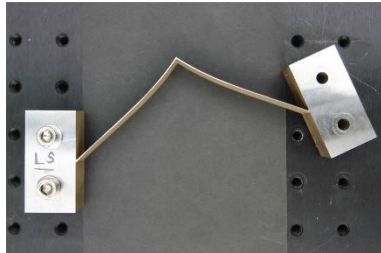


(b) Assembled.



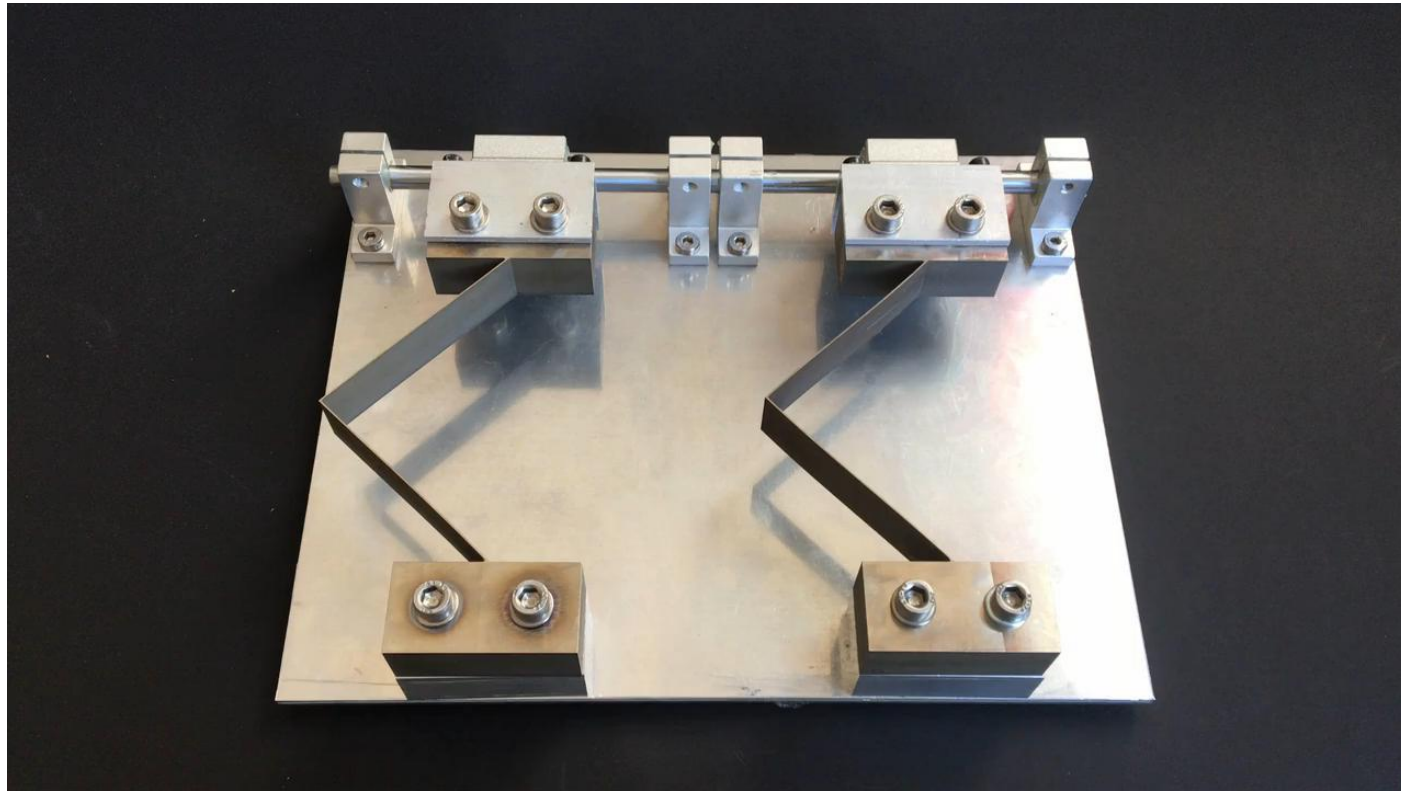
(c) After +30 mm displacement.

(d) After -30 mm displacement.



28% reduction in peak stress

Initial stress or curve



Static balancing

Increase range of motion:

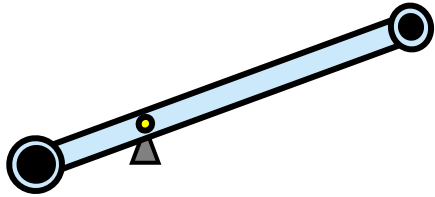
- Series-parallel
- Initial stress or curve

Increase stiffness ratio:

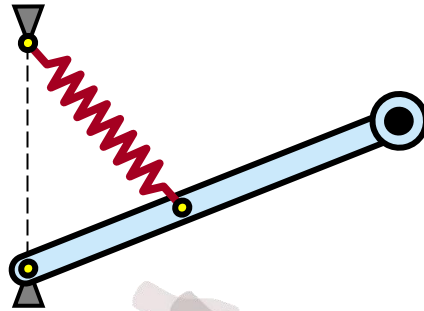
- **Reduce k_f : static balance**
- Increase k_s : reinforcement

Static Balancing

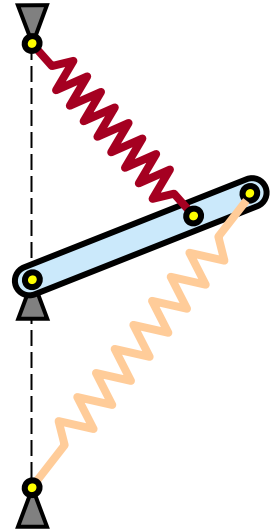
All conservative forces can be cancelled out!



Meager Bridge (Amsterdam)



Anglepoise™

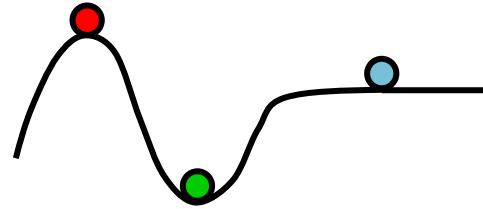


Wilmer™

Static Balancing

All conservative forces can be cancelled out!

- Continuous equilibrium
- Constant potential energy
- Neutral stability



Meager Bridge (Amsterdam)

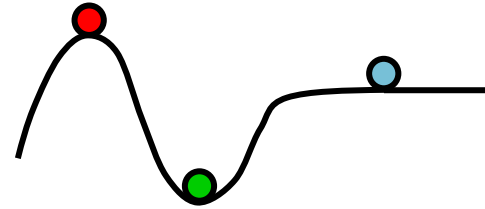
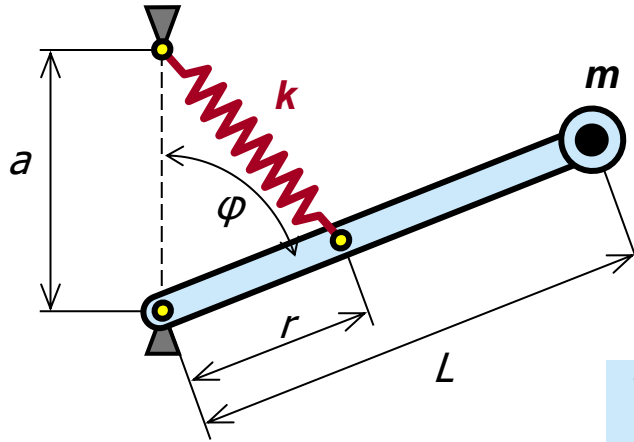


Anglepoise™



Wilmer™

Constant potential energy



Assuming zero-free-length springs:

$$\bar{F} = k\bar{\ell}$$

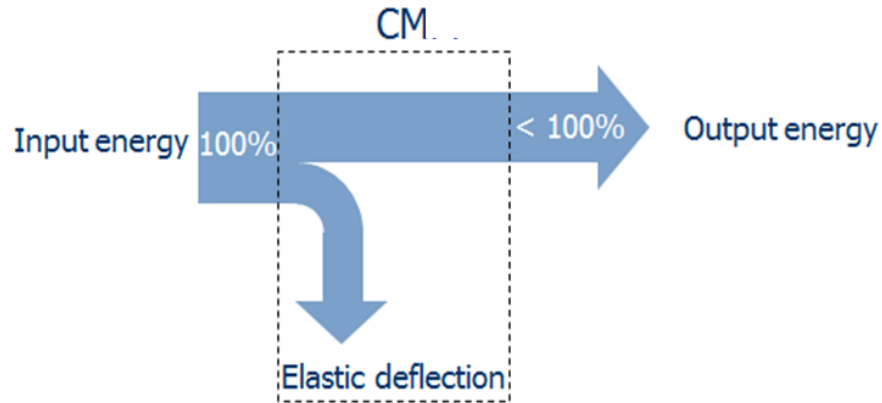
$$V_m = mgL \cos \varphi$$

$$V_s = \frac{1}{2}k\ell^2 = \frac{1}{2}k(a^2 + r^2) - kar \cos \varphi$$

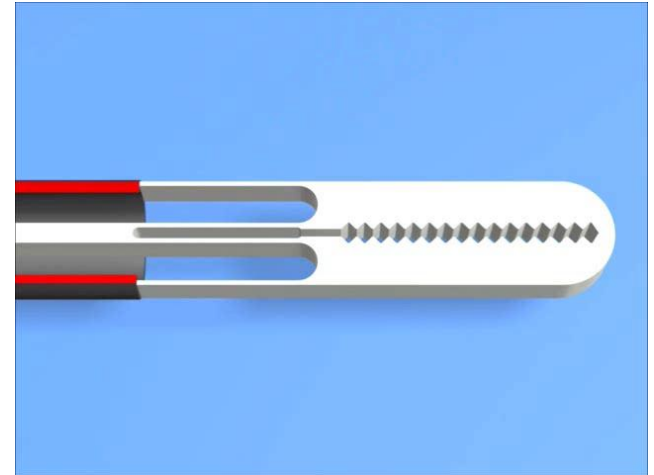
$$V_{tot} = c_{nst} + (mgL - kar) \cos \varphi$$

$$\text{Condition : } mgL = kar$$

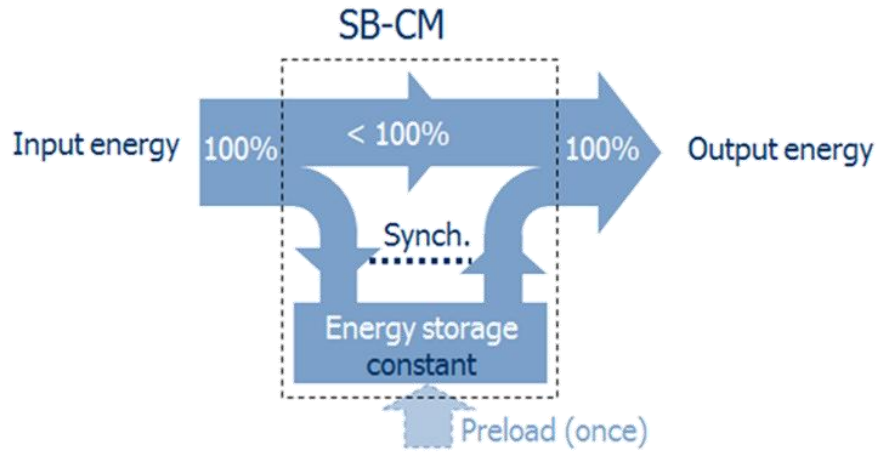
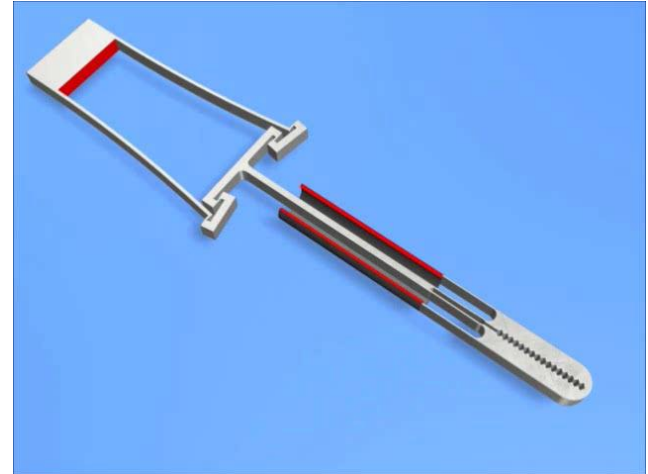
Static balance



Motion → elastic deformation → energy → motion stiffness

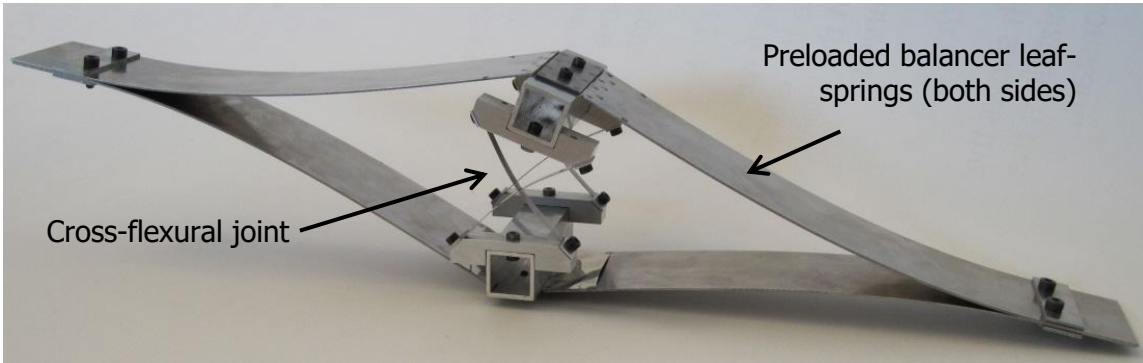
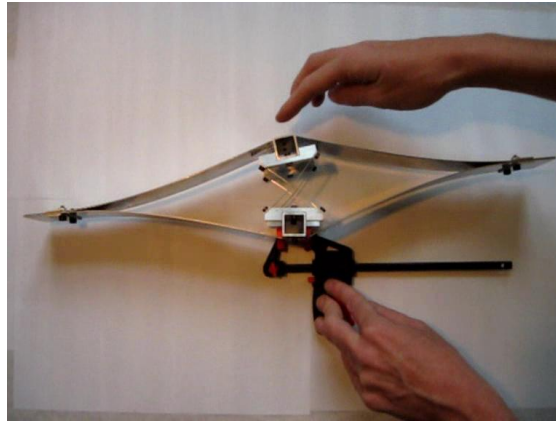
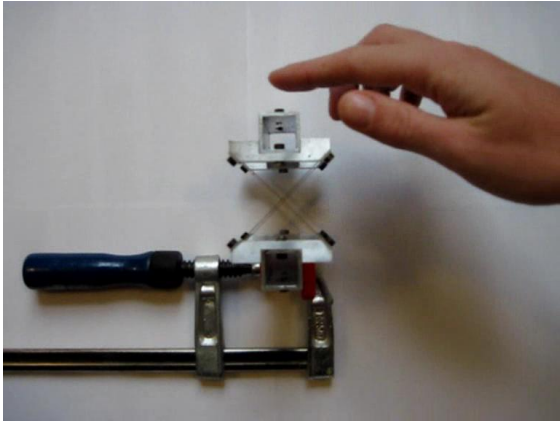


Static balance

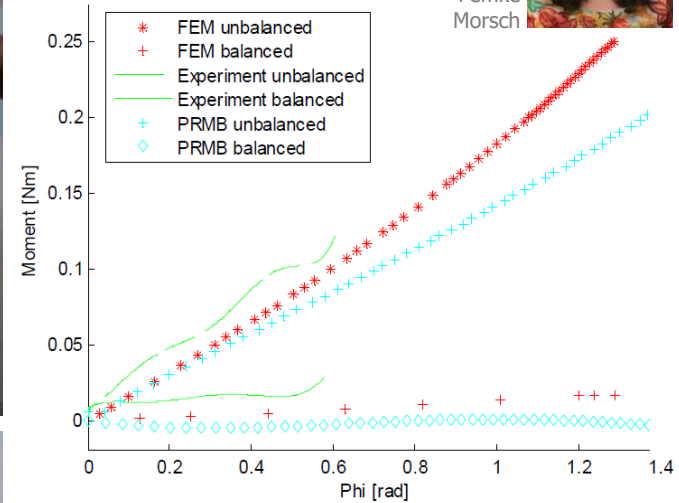


Constant total potential energy \rightarrow net zero motion stiffness

Static balance

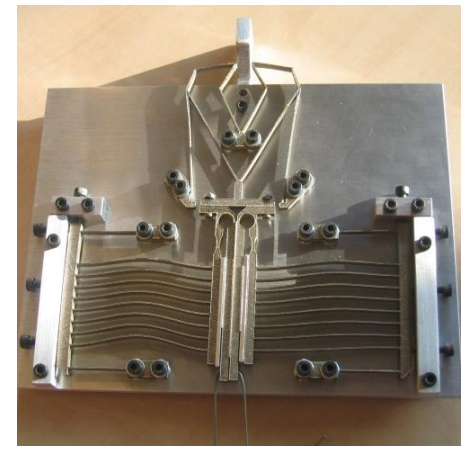
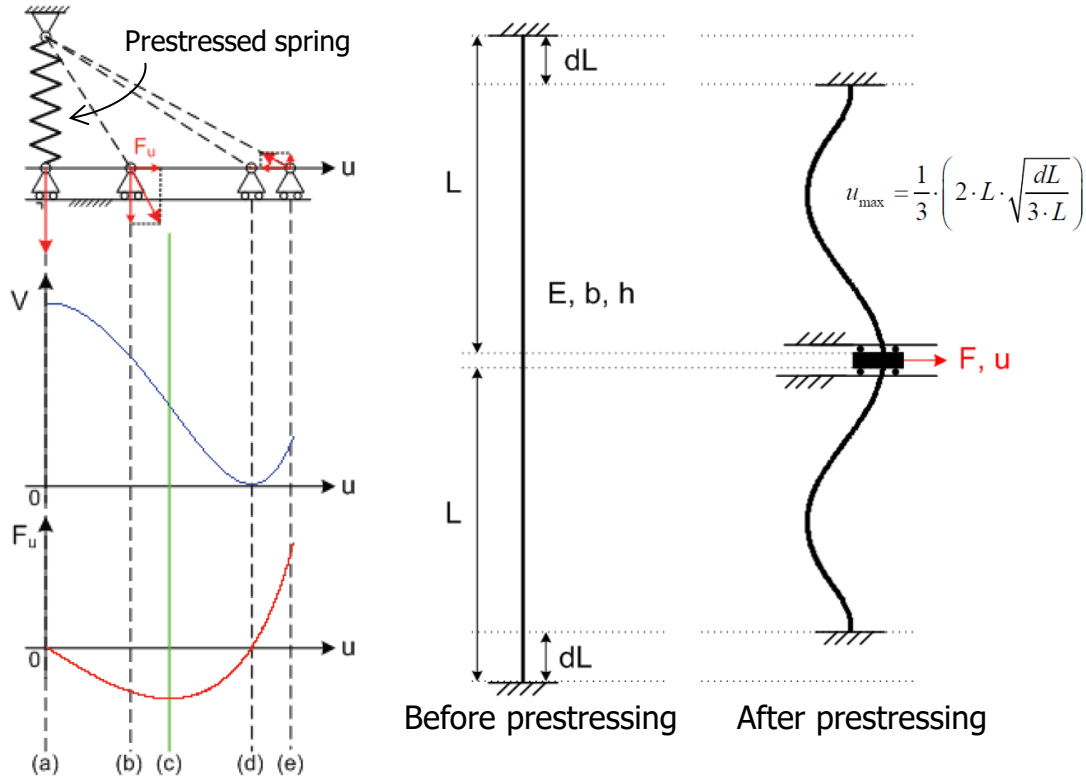


Femke Morsch 



	Average moment reduction, $\varphi = 0$ -end trajectory [%]	Max moment reduction, $\varphi = 0$ -end trajectory [%]	End trajectory [rad]
PRBM	95	98	1.42
FEM	93	93	1.28
Experiment	70	63	0.58

Static balance

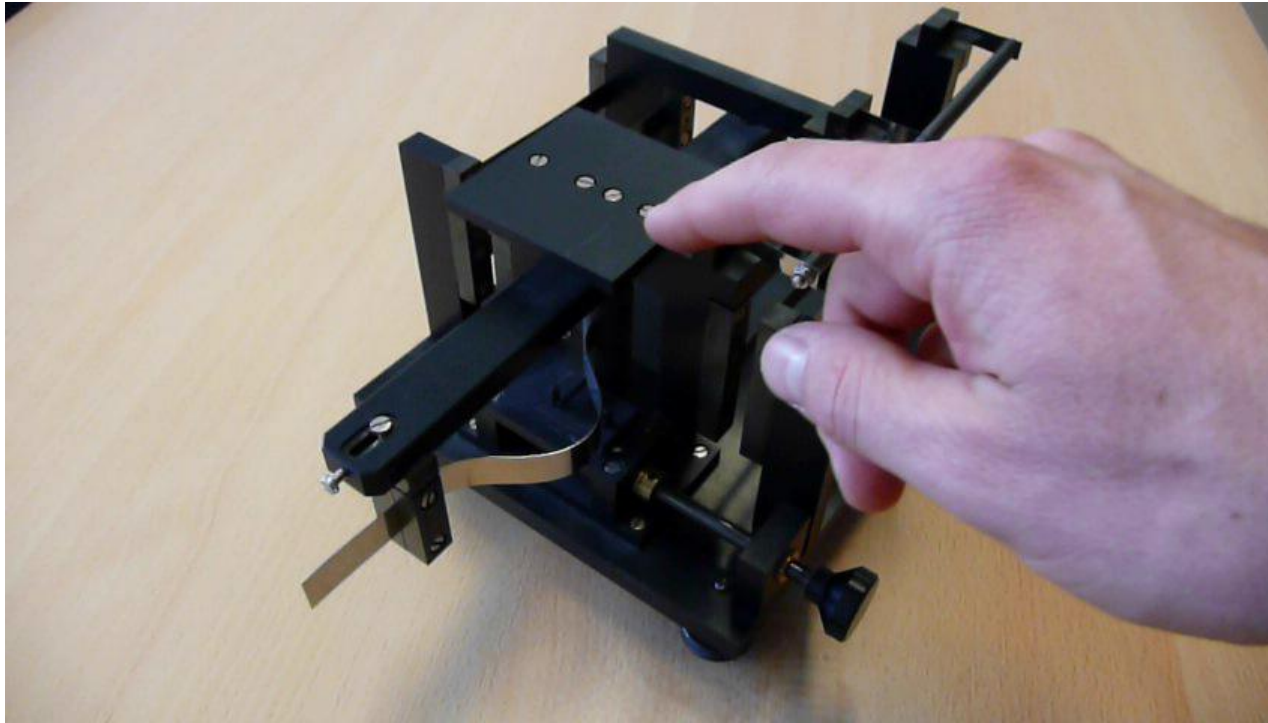


Statically balanced gripper

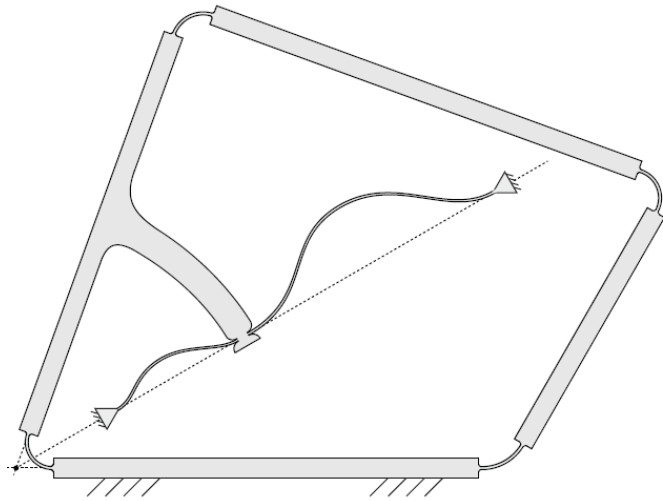
Karin Hoetmer, Charles Kim,
Geoffrey Woo, Just Herder
2009

Delft University of Technology
Bucknell University

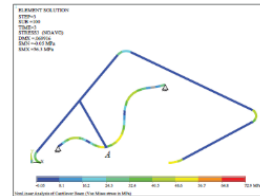
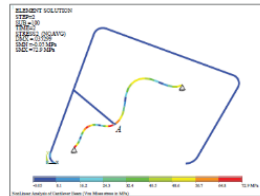
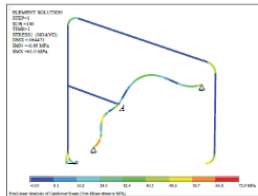
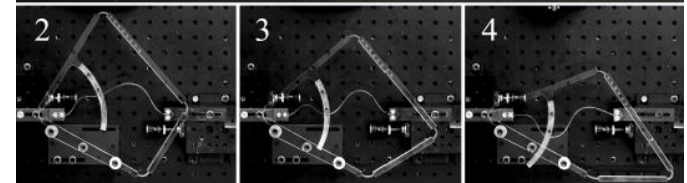
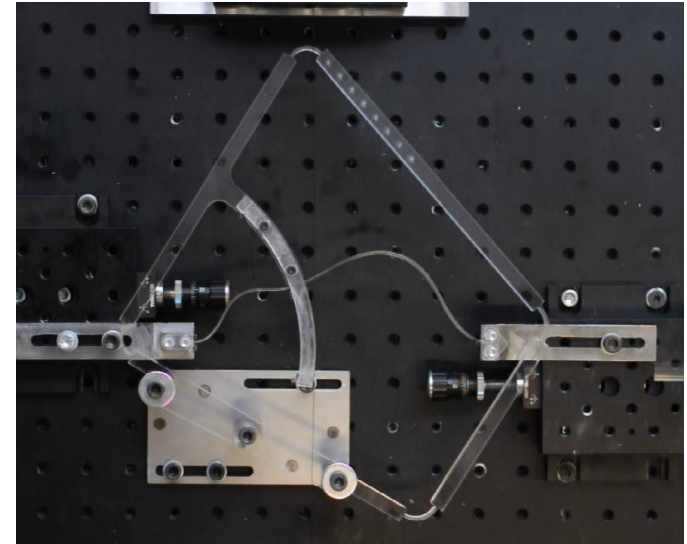
Static Balancing of Compliant Mech.



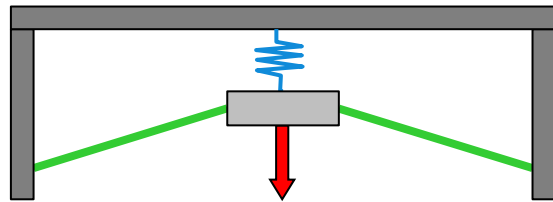
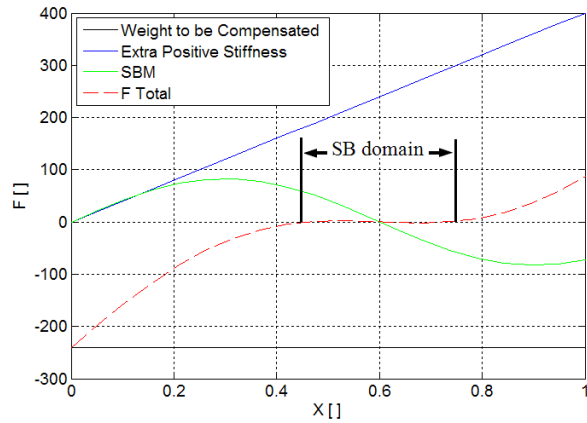
Static Balancing of Compliant Mech.



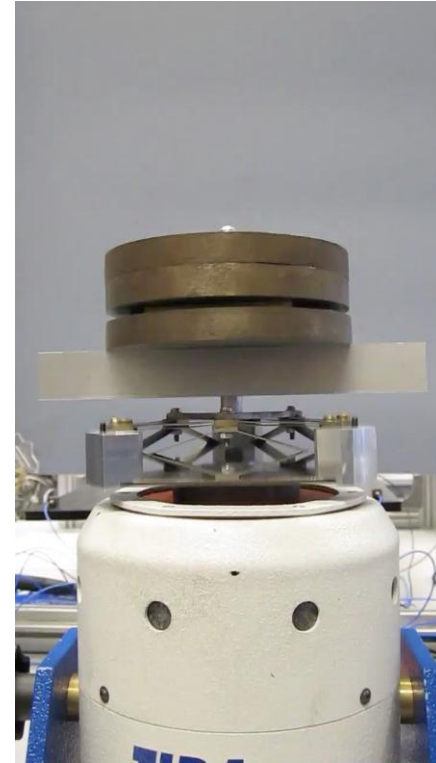
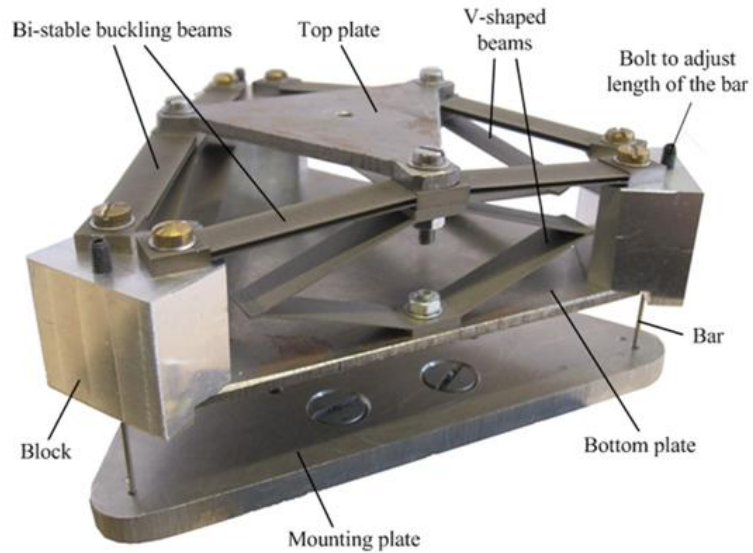
Luc Berntsen
Daan Gosenshuis



Constant force unit

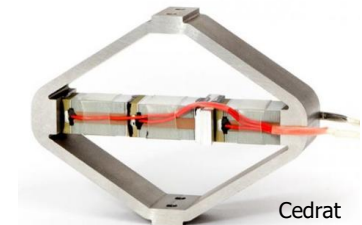


Vibration Isolator

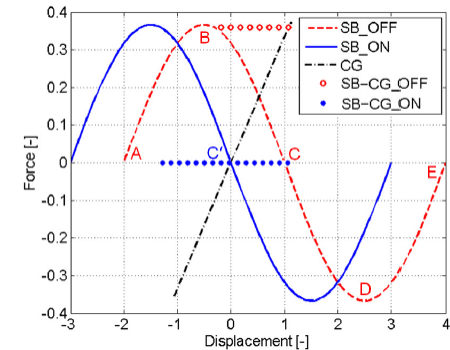
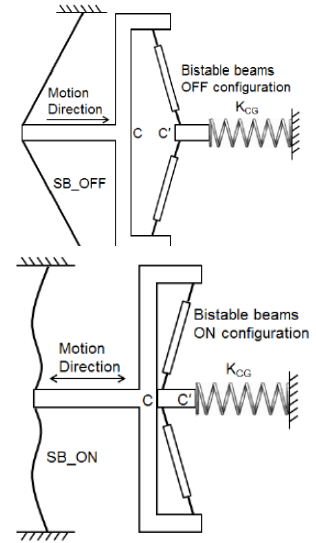
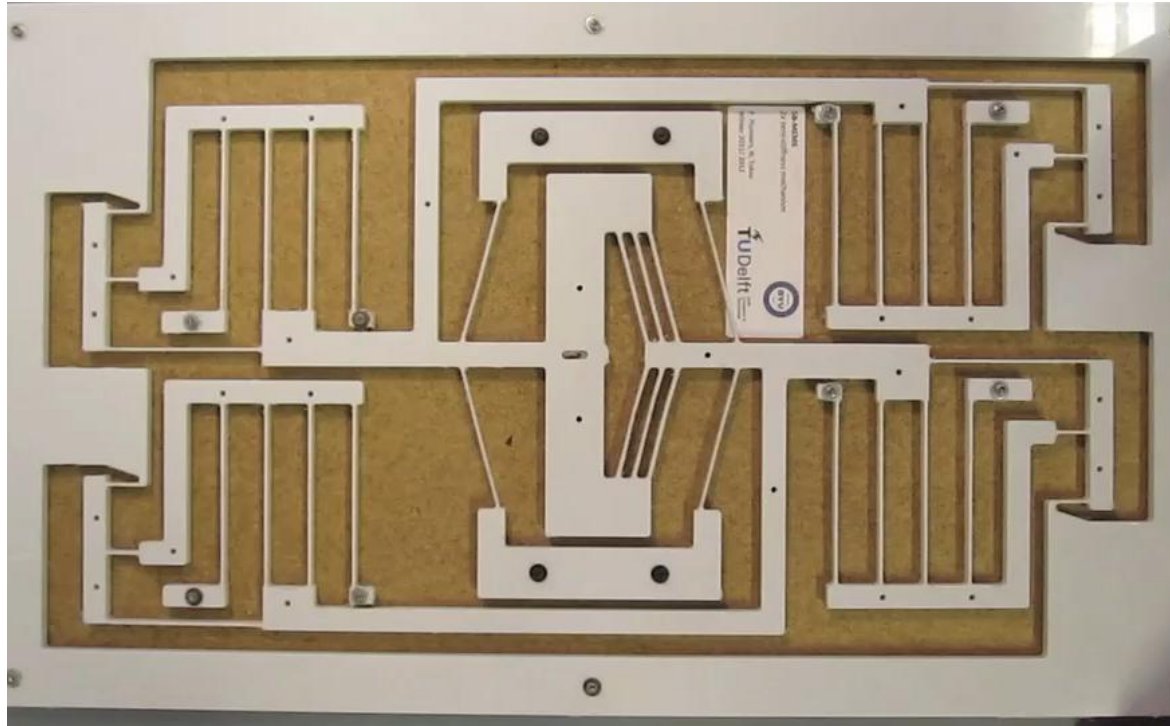


Advantages of static balancing

- Reduced operating effort
 - Less energy consumption
 - Less heat generation
 - Increased safety
- Pure force transmission (signal)
- System efficiency, e.g. elastic transmission in actuators
- Eliminate backlash by preloading
- Vibration isolation
- Extreme anisotropy, approximate conventional joints
- ...



Switchable static balance

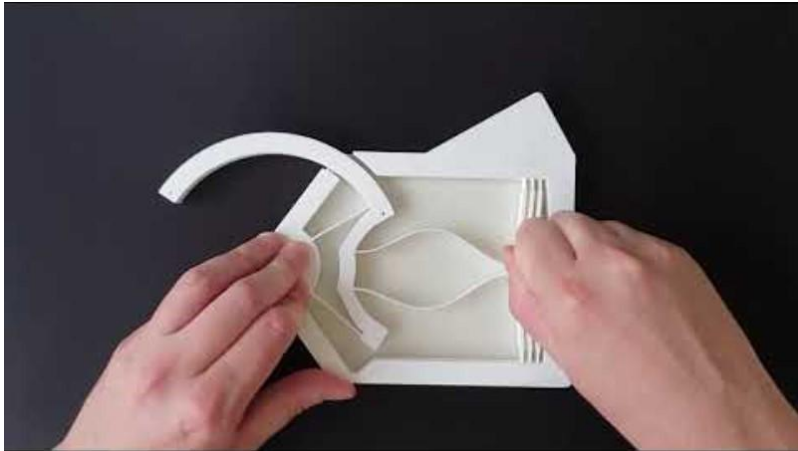


Switchable static balance

Reinier
Kuppens



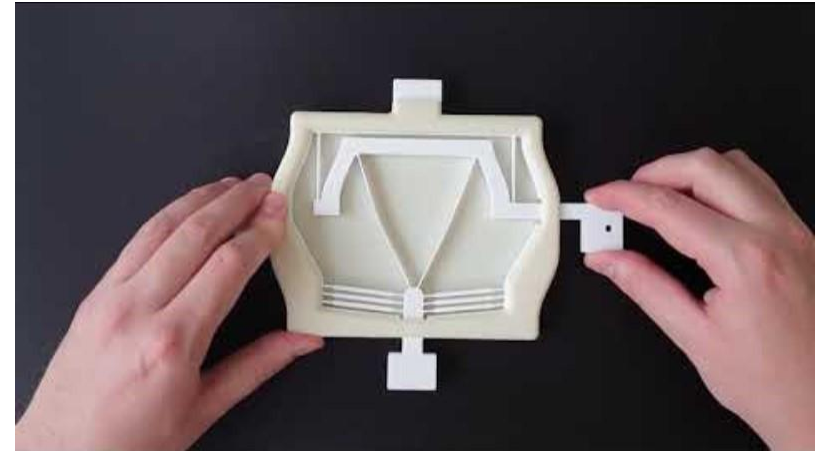
Switchable revolute unit cell



https://www.youtube.com/watch?v=T5wnomW_CJE

1.9M views

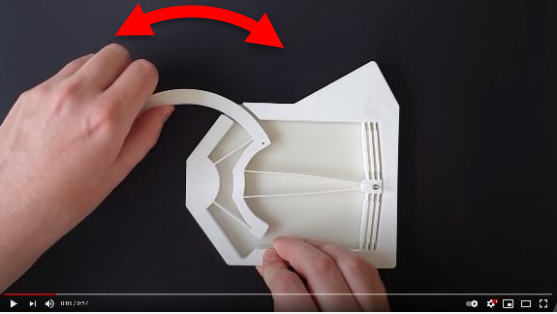
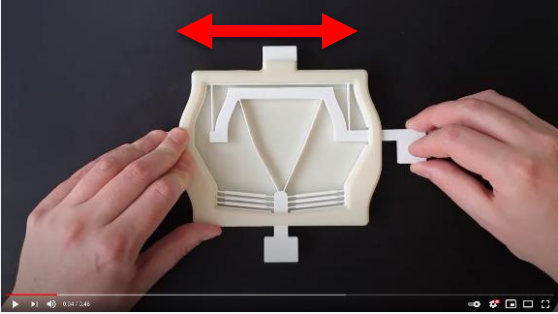
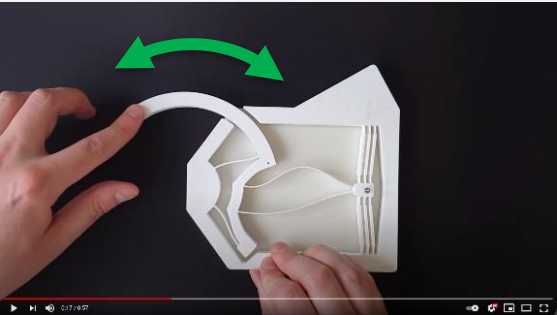
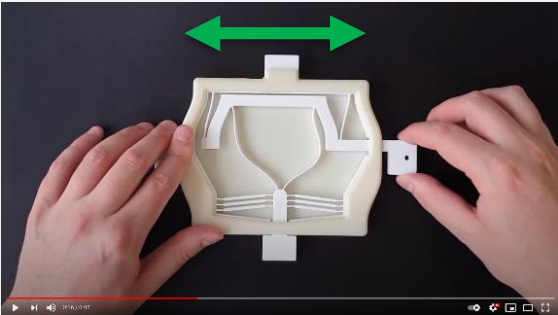
Switchable prismatic unit cell



<https://www.youtube.com/watch?v=X2tRcEME14w>

Soft mode is more than three orders of magnitude more compliant than stiff mode

Switchable static balance

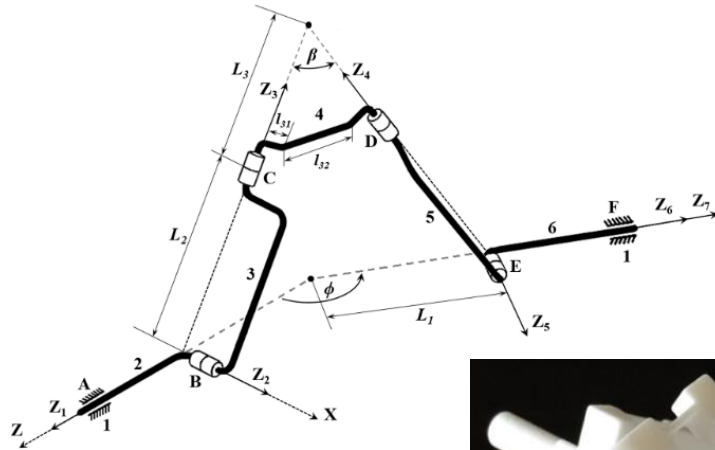
	Revolute unit cell	Prismatic unit cell
Stiff mode (locked, "off")	 A hand holds a white, curved, fan-like structure. A red double-headed arrow above it indicates a small range of motion. The structure is shown in a locked state.	 A hand holds a white, box-like structure with internal struts. A red double-headed arrow above it indicates a small range of motion. The structure is shown in a locked state.
Soft mode (free, "on")	 A hand holds the same white, curved structure. A green double-headed arrow above it indicates a much larger range of motion. The structure is shown in a free state.	 A hand holds the same white, box-like structure. A green double-headed arrow above it indicates a much larger range of motion. The structure is shown in a free state.

Three orders of magnitude more compliant

Spatial arrangements

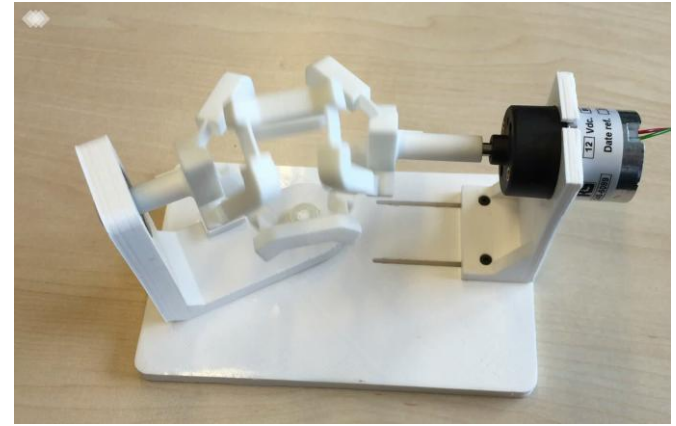


Davood Farhadi



Bennett 6R hybrid linkage

Fully compliant constant velocity coupling

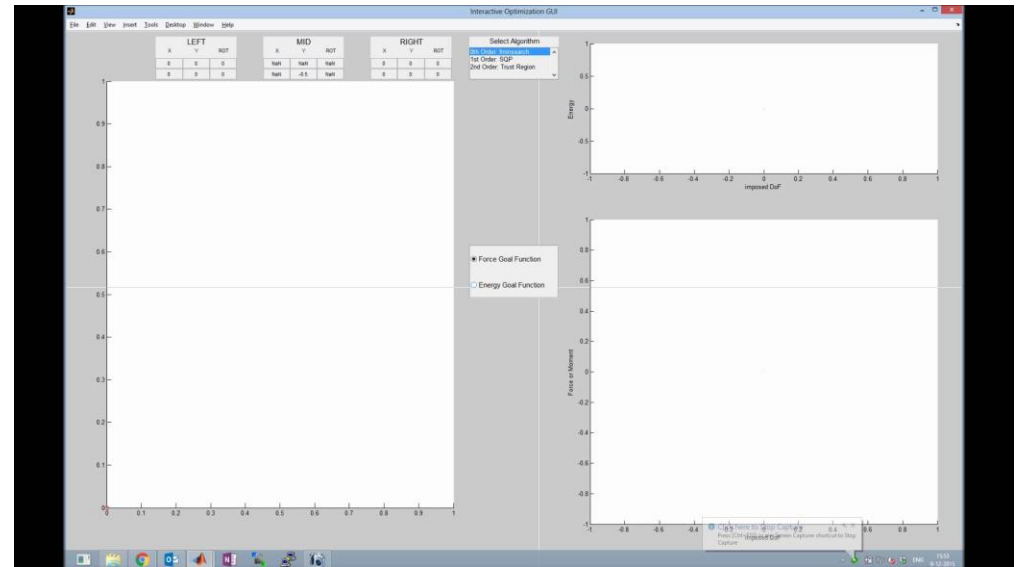
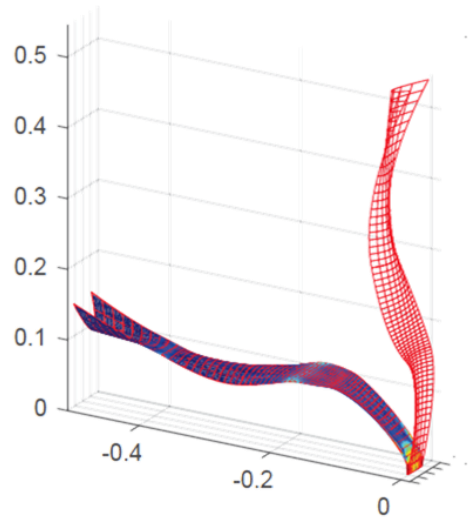


Shell mechanisms



Giuseppe Radaelli

Spatial compliant mechanisms
Tailored stiffness
Analysis and synthesis



Eigendecomposition



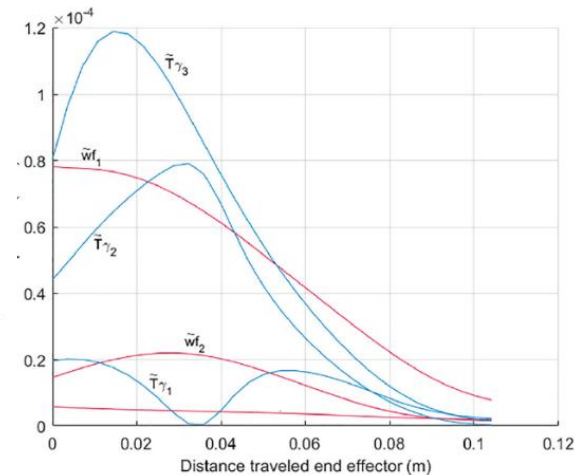
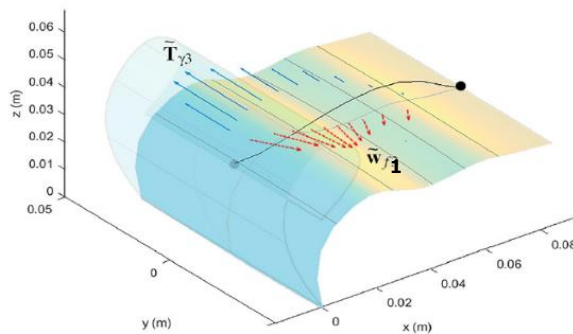
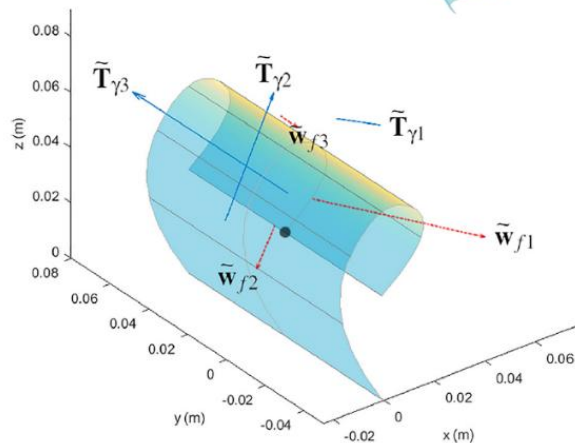
Joost Leemans



Werner van de Sande



$$\tilde{a}_{f_i} = \frac{\delta_{eq_i}}{F_{eq_i}} = \left(h_i^2 + |r_i|^2 \right) \frac{\theta_i}{M_i}$$



Shell building blocks

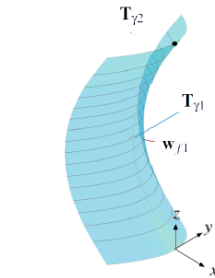
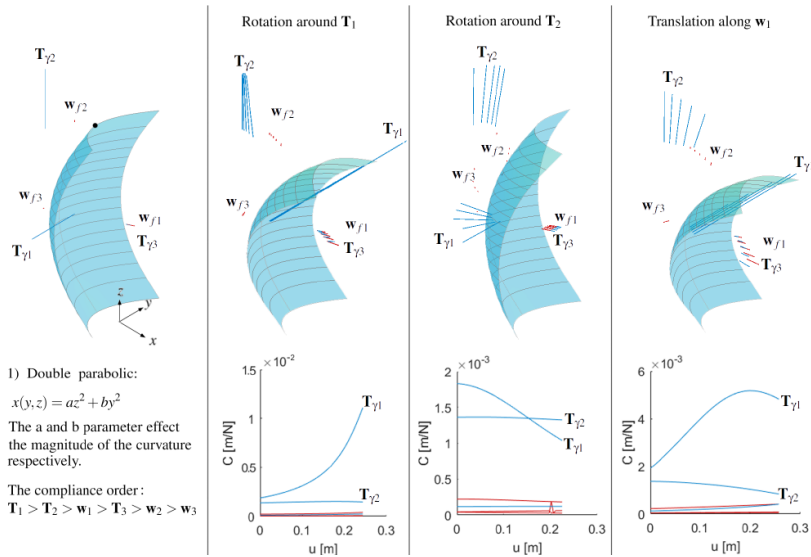


Joost Leemans

Werner van de Sande

Double parabolic

Hyperbolic parabolic

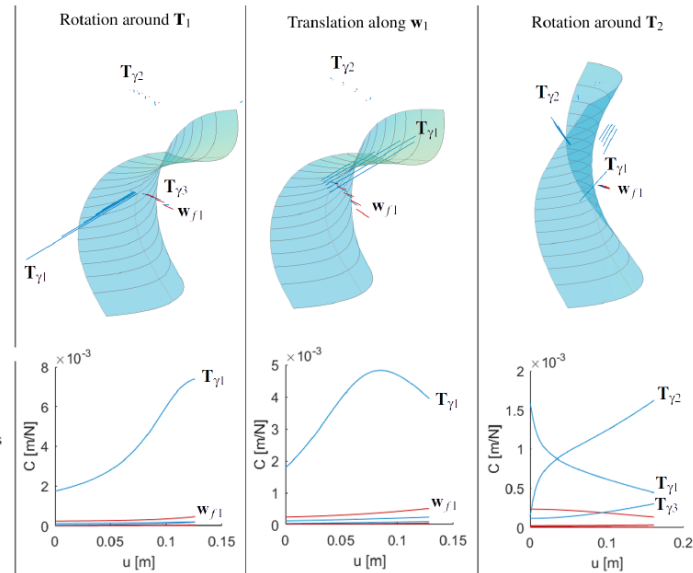


Hyperbolic parabolic:

$$x(y, z) = az^2 - by^2$$

This surface has two parameters a and b effecting the magnitude of opposing curvatures.

The compliance order:
 $T_1 > T_2 > w_1 > T_3 > w_2 > w_3$



Shell building blocks

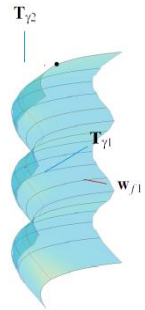


Joost Leemans



Werner van de Sande

Double corrugated

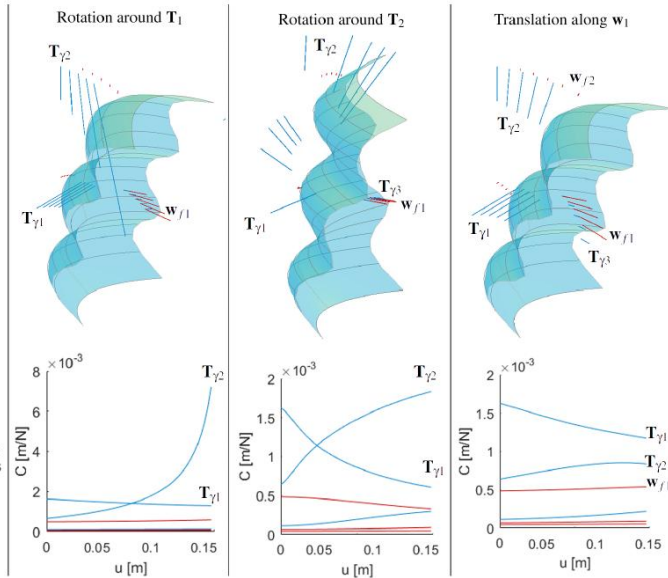


Double corrugated shell:

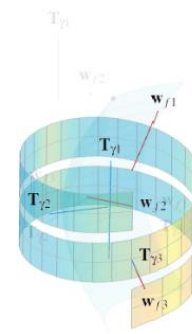
$x(y, z) = ay^2 - c \cos\left(\frac{n\pi z}{d}\right) + ab^2$
 where a is the amplitude of the second curve in xy plane, b is half the width and c is determines the corrugation amplitude and n is the amount of semi whole waves.

The compliance order:

$T_1 > T_2 > w_1 > T_3 > w_2 > w_3$



Helix



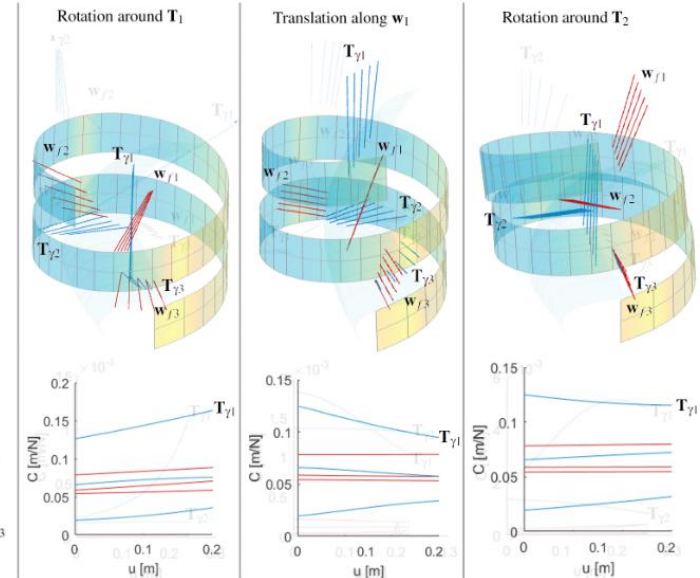
The Helix: parabolic:

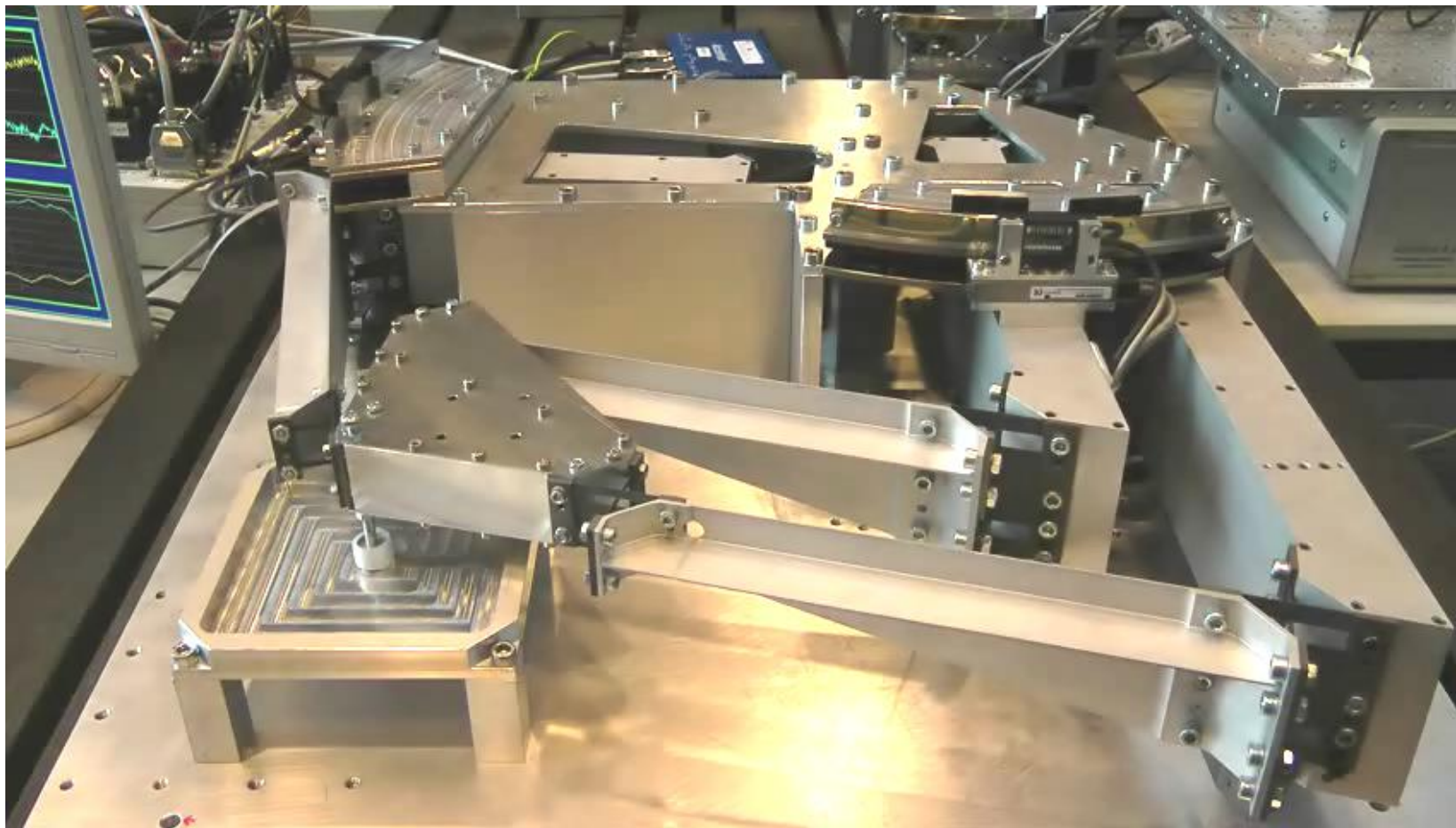
$$x(u, v) = a \cos(v)$$

$y(u, v) = a \sin(v)$ meter effect
 $z(u, v) = cv + u$ the curvature respectively.

The compliance order:

$T_1 > w_1 > T_2 > T_3 > w_2 > w_3$





New book and website

THEME – INITIATIVE BY DUTCH UNIVERSITIES AND DSPE IN COLLABORATION WITH INDUSTRY

UPDATING DDP

An initiative to produce updated design principles for precision mechatronics has been developed by Dutch universities of technology in association with DSPE, in close collaboration with the Dutch high-tech industry. Building on the legacy of Wim van der Hoek, the Dutch doyen of design principles, the aim of the initiative is to collect over 100 cases that demonstrate the proper application of contemporary design principles. The cases will be presented on a dedicated website and collected in a new textbook, preceded by an extensive, in-depth introduction of the design principles.

Initiators

The initiative to update the design principles for precision mechatronics came from the professors of precision engineering and mechatronics at the three Dutch universities of technologies – Delft, Eindhoven and Twente – in association with DSPE.



From left to right:
Dannis Brouwer is professor of Precision Engineering at the University of Twente, Enschede (NL).
Just Herder is professor of Interactive Mechanisms and Mechatronics at Delft University of Technology, Delft (NL).
Pieter Kappelhof is vice president of DSPE, director of Technology at Hittech Group, located in Den Haag (NL), and hybrid teacher of Opto-mechanics at Eindhoven University of Technology (TU/e), Eindhoven (NL).
Hans Vermeulen is part-time professor of Mechatronic System Design at TU/e and senior principal architect EUV Optics System at ASML, located in Veldhoven (NL).

PIETER.KAPPELHOF@DSPE.NL / J.P.M.B.VERMEULEN@TU.E.NL

DPPM Cases

Design Principles for Precision Mechatronics. A collection of applications categorized in themes known from construction principles.

How to design mechanical hardware as part of a modern precision mechatronic system.

The precision mechatronics community has a long history of continuous updates on DDP ("Des Duivels Prentenboek") content by Wim van der Hoek and his 'heritage keepers'. It is considered relevant to prolong this process with new examples from the field of precision mechatronics, incl. opto-mechanics, electro-mechanics and material science.

In the coming year(s), we write a book and a website containing examples of precision mechatronics elements. DSPE members can contribute by writing clear examples to be freely used. Company and designer can be mentioned. Examples should not be complete systems.

Overview of the design principles for accuracy and repeatability, as of ~1970, and their evolution, as of ~2000 (in green) and ~2010 (in red).

Design principle	Implementation
Kinematic design	<ul style="list-style-type: none">▶ Exact constraints▶ Mechanical decoupling via flexures and elastic hinges
Design for stiffness	<ul style="list-style-type: none">▶ Structural loops with high static stiffness and favourable dynamic stiffness
Lightweight design	<ul style="list-style-type: none">▶ Design for low mass and high eigenfrequencies
Design for damping	<ul style="list-style-type: none">▶ Energy dissipation that slows down motion without introducing position uncertainty
Design for symmetry	<ul style="list-style-type: none">▶ Symmetry in geometry and external loads▶ Over-actuation
Design for low friction and hysteresis	<ul style="list-style-type: none">▶ Minimisation of friction and virtual play in high-precision structures, connections and guideways
Design for low sensitivity	<ul style="list-style-type: none">▶ Thermal centre and thermal (compensation) loops with high stability▶ Low-expansion materials▶ Isolation of disturbances, e.g. via isolated metrology loop▶ Offset minimisation, e.g. Abbe principle and Bryan principle, and drive-offset minimisation relative to the centre of mass▶ High-bandwidth feedback control
Design for stability	<ul style="list-style-type: none">▶ Minimisation of heat dissipation and microslip in interfaces▶ Minimisation of material creep and drift
Design for load compensation	<ul style="list-style-type: none">▶ Weight compensation, reaction force compensation and (parasitic) stiffness compensation▶ Position-dependency compensation
Design for minimal complexity	<ul style="list-style-type: none">▶ Balancing and hence minimisation of complexity and related cost via a multidisciplinary system approach

Design principles

- 1 Introduction
- 2 Kinematic design
- 3 Design using flexures
- 4 Design for static stiffness
- 5 Design for dynamic stiffness
- 6 Design for damping
- 7 Design for low friction and hysteresis
- 8 Design for stability
- 9 Design for low sensitivity
- 10 Design for load compensation

Conclusion

Improve behavior

- Initial stress or curve
- Reduce k_f : static balance
- Increase k_c : reinforcement

Future trends

- Combination of above techniques
- Methods for 3D compliant mechanisms
- Mechanical metamaterials
- Topology opt. (large defl., stat. balance)
- High loads & large deflection
- Alternative manufacturing, e.g. origami

